

ModHel'X: an approach to multi-formalism modeling

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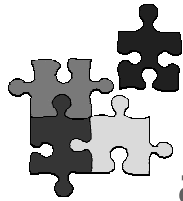
■ Context

- ▶ **Modeling** the behavior of **heterogeneous systems**
 - Software/hardware, digital/analog, internal/external IPs...
- ▶ Using **different models** to represent **one system**
 - Level of refinement, focus aspects (NFP...),
Domain Specific Modeling Languages (DSMLs)

Русский 精忠

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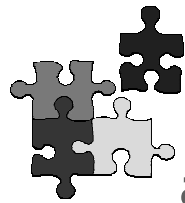


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Multi-formalism modeling =
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■ What for ?

- ▶ **Simulation**, code generation, verification, validation, tests...
- ▶ Maximize **model reuse**, facilitate and optimize **designers collaboration**

■ Main issues

- ▶ Describe **the semantics of a modeling language** precisely
- ▶ Define **the semantics of a combination of modeling languages** in a model

- **Kermeta** [Muller05]: meta-programming language allowing to **define the semantics of a modeling language using UML meta-models**
- **ATOM³** [deLara02]: **meta-model transformation** tool for multi-paradigm modeling
- **Ptolemy II** [Lee03]: **heterogeneous modeling** framework based on the **model of computation** concept, with a **component-oriented** abstract syntax
- **BIP** [Sifakis06]: language for defining **heterogeneous interactions**, with formal properties for **verification**
- **Tagged Signal Model** [Lee98]: mathematical framework for comparing models of computation, no execution purpose
- **Rosetta** [Kong03]: heterogeneous modeling framework with a denotational semantics, implements the **facets concept**

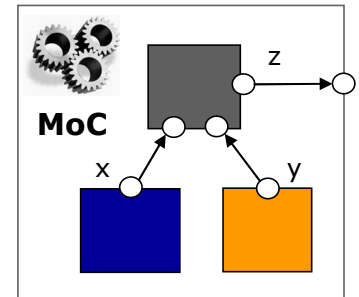
■ Vocabulary

► Modeling language = structure + semantics

- UML meta-model + execution operations (imperative semantics)
- or
- Fixed (component-oriented) abstract syntax + Model of Computation

► Model of computation (MoC)

- Set of rules that define the behavior of the model by **combining** the behaviors of its components
- = description of the “**computation and communication features**” of a modeling language



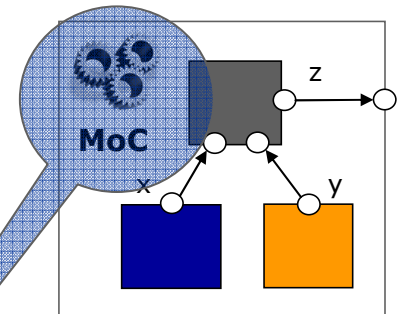
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■ Objectives

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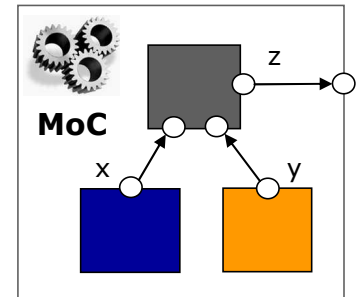
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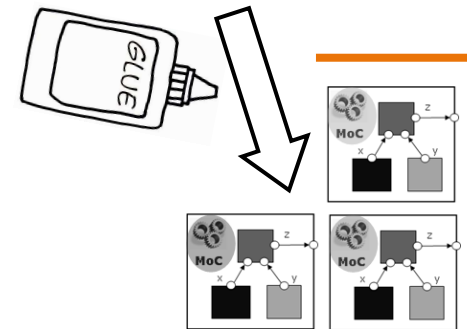
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■ Objectives

- Allow a precise description of
 - the semantics of models of computation
 - the semantics of their interactions (the “glue” !)
- Provide support for the interpretation of compositions of MoCs in order to allow the execution of heterogeneous models





Main principles

■ Encapsulation



- ▶ Components of a model = **black-boxes** with well defined **interfaces**
 - Goal: **decouple the internal mechanism of a component** from the model in which it is used

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- ▶ Execution of a model = observations of its behavior = **snapshots**
 - Triggered by time, environment changes and by components of the model
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■ Hierarchy & delegation



- ▶ Behavior of a component = internal model + internal MoC
- ▶ Update of a component = **update of its internal model**
- ▶ **Semantic adaptation at the border** of the component



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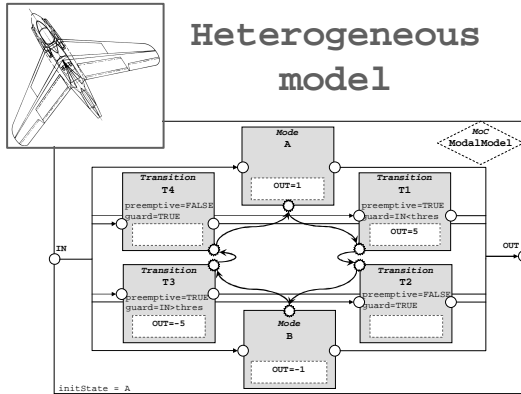
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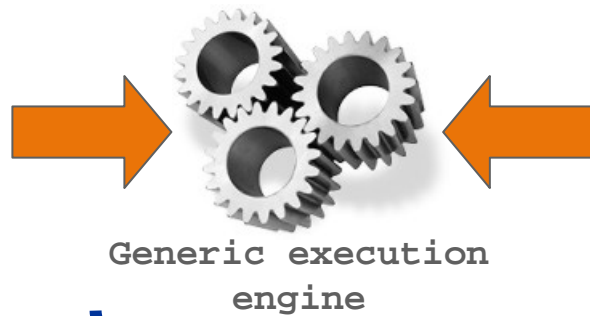
one MoC by layer + local heterogeneity = reduced complexity

General architecture of ModHel'X

Heterogeneous model



Generic meta-model
for the representation of
the structure of
heterogeneous models

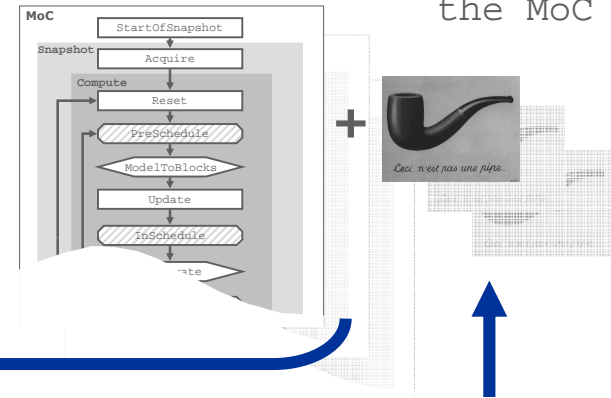


Generic algorithm
for executing
heterogeneous models

Executable descriptions
of each MoC =

Generic model of
execution

Semantics of
the MoC

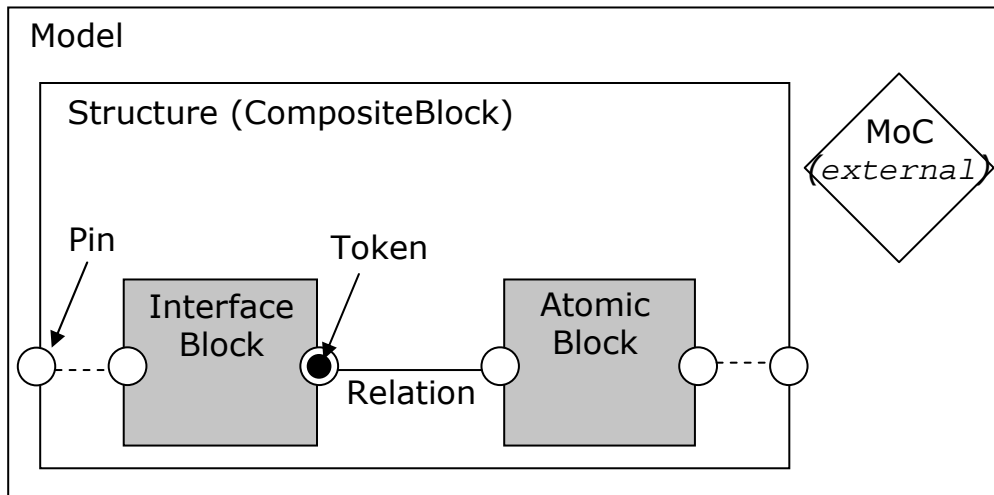


Language for describing

- ◆ The operational semantics of a MoC
- ◆ The interactions between MoCs

Representing an heterogeneous model

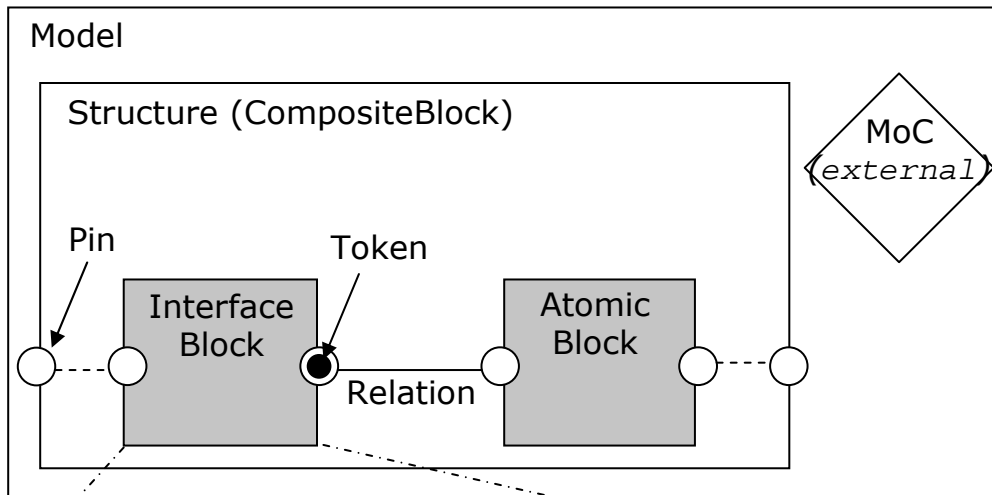
- A set of few basic and generic objects



- Two separate aspects
 - ▶ **Structural:** Blocks, Pins, Relations, Tokens
 - ▶ **Behavioral:** Model of computation
- **Specialization** of these objects for each MoC

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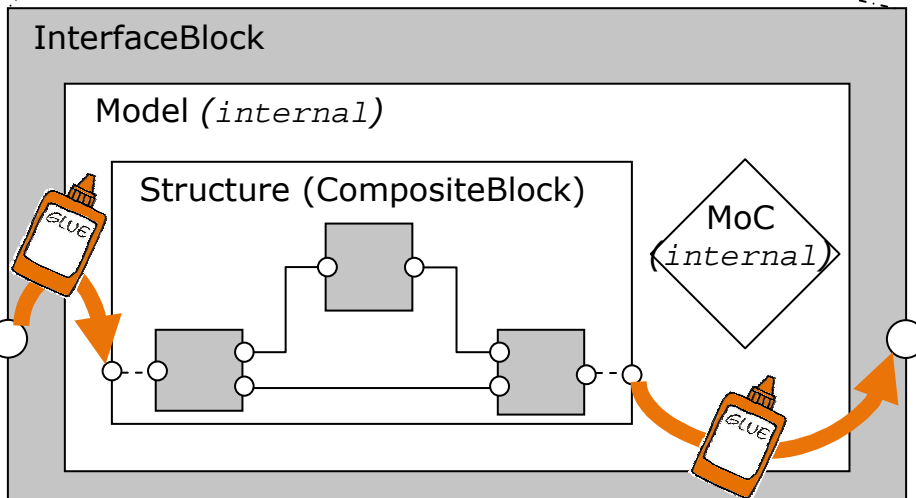
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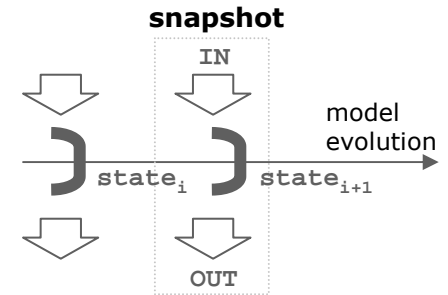
- Hierarchical heterogeneity

- ▶ An **InterfaceBlock** has an internal model
- ▶ The internal & the external MoCs can be different
- ▶ The InterfaceBlock **realizes the semantic adaptation**

Executing an heterogeneous model

■ One **execution** =

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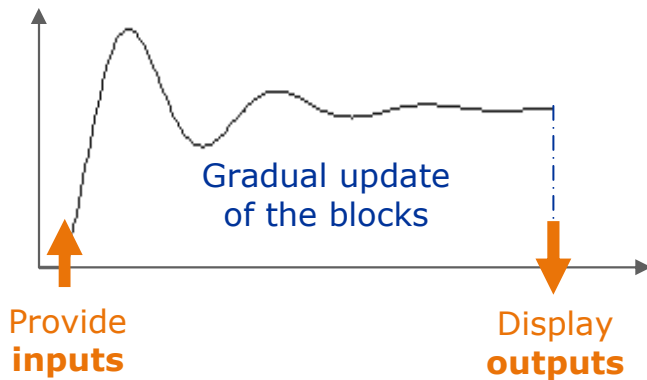
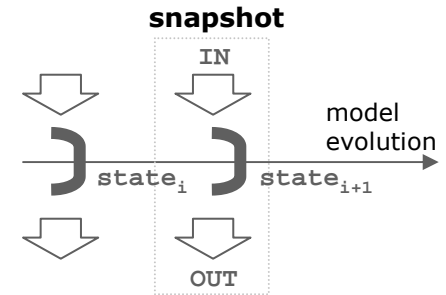


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▶ Causal execution

- $State_i + \mathbf{inputs}_i \rightarrow \mathbf{outputs}_i + State_{i+1}$

▶ Gradual update of the model blocks

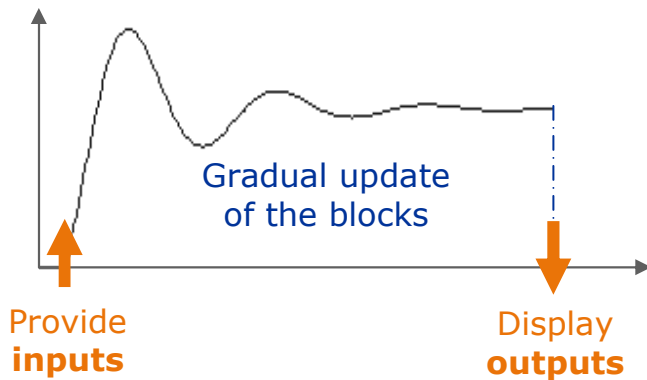
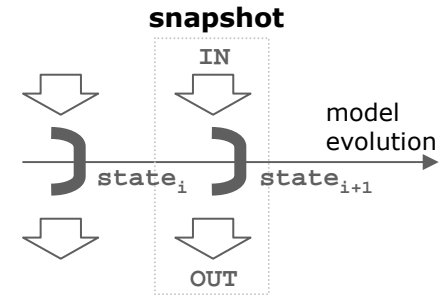
- **Schedule** of the block to update
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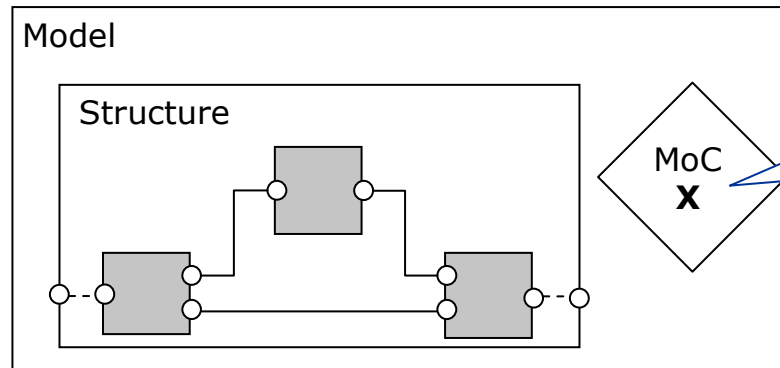
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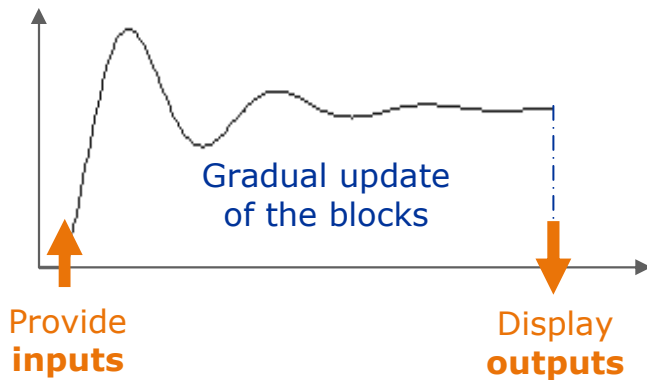
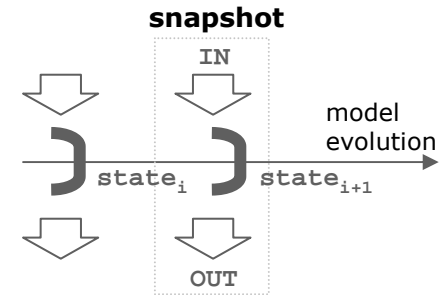
For this example,
the considered
MoC is of the
« data-flow » type

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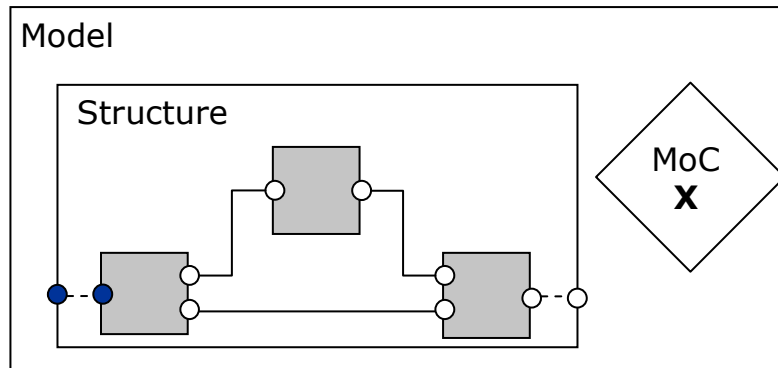
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Provide inputs

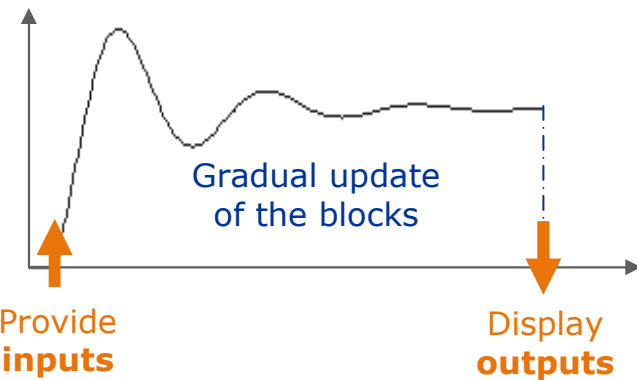
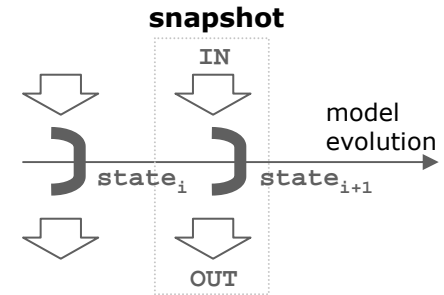


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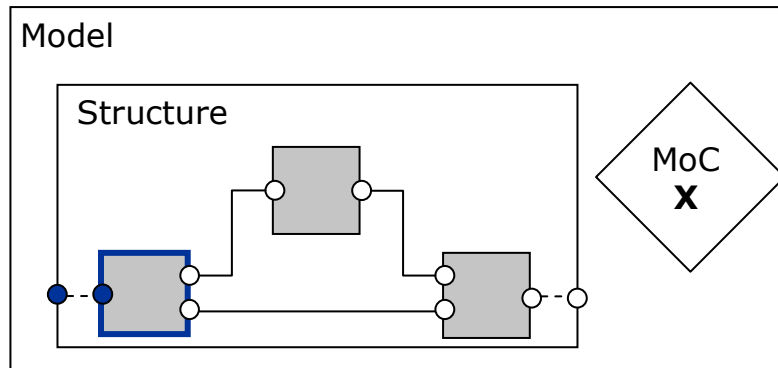
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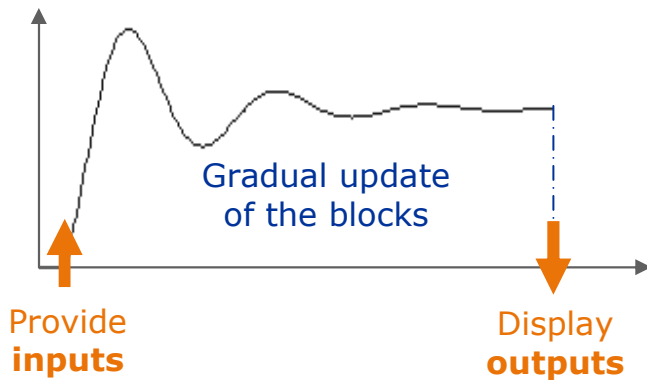
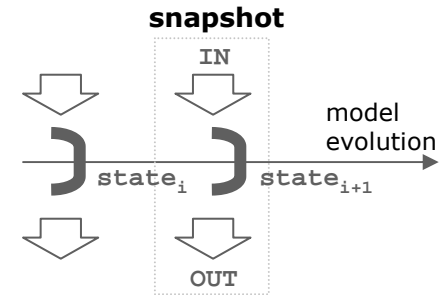


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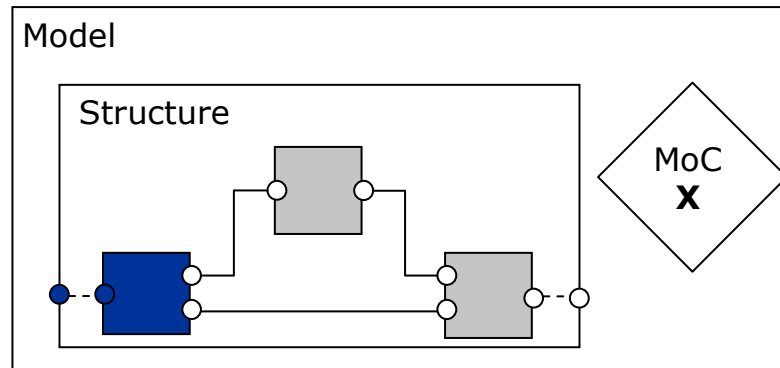
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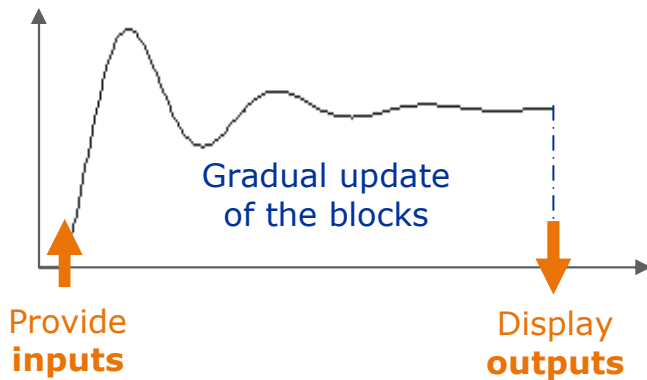
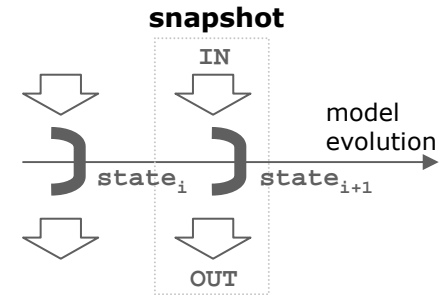


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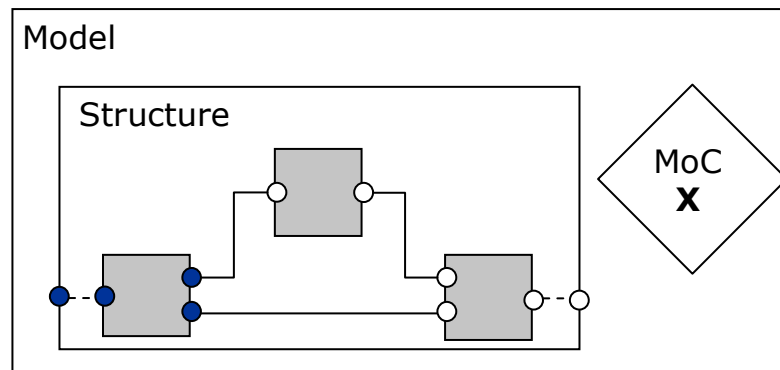
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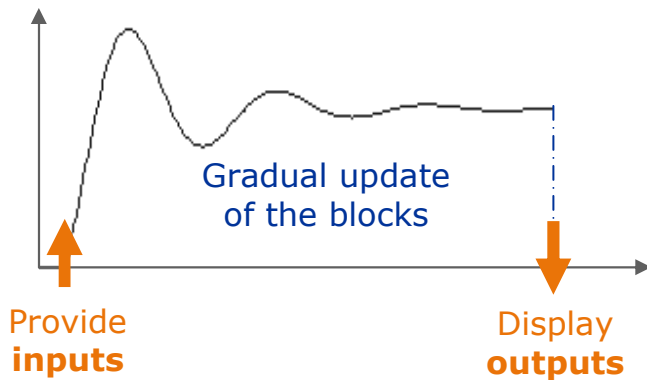
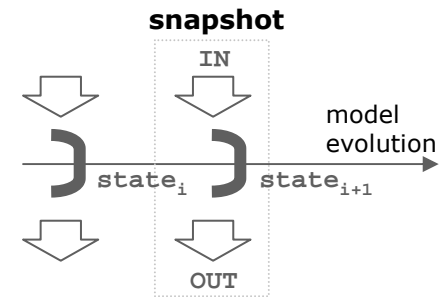


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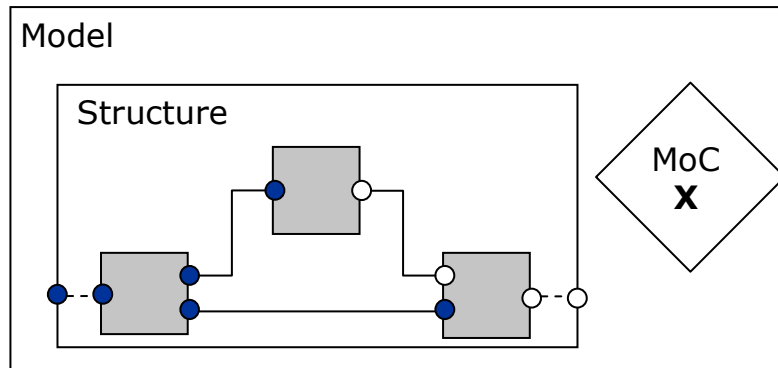
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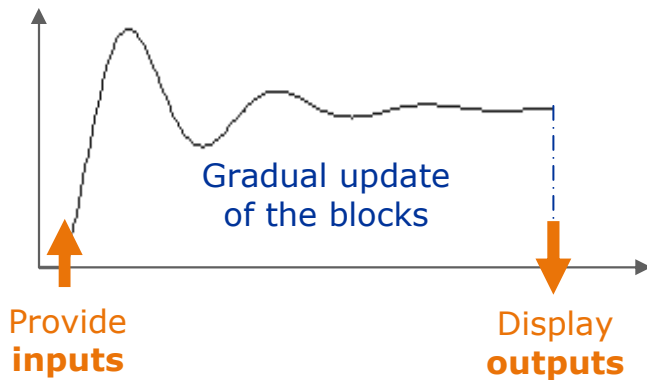
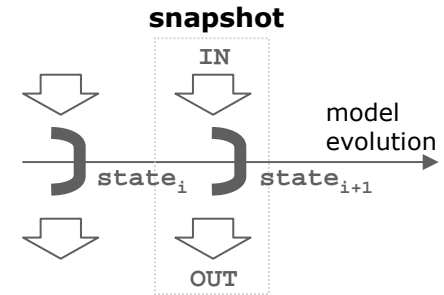


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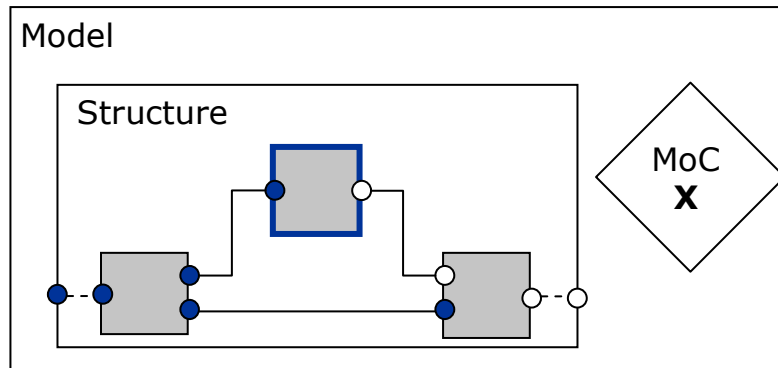
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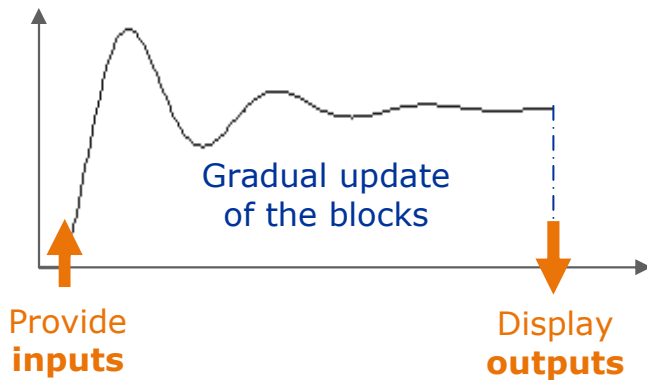
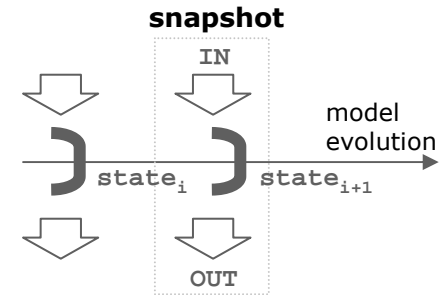


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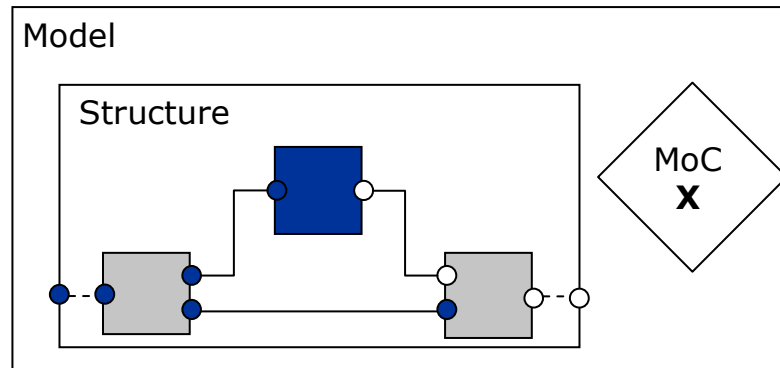
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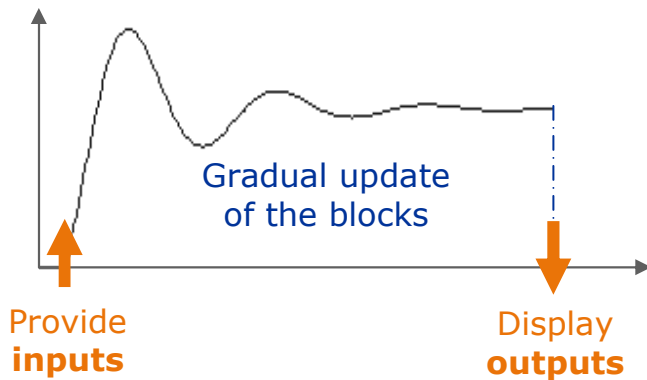
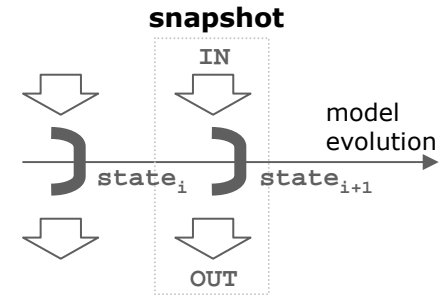


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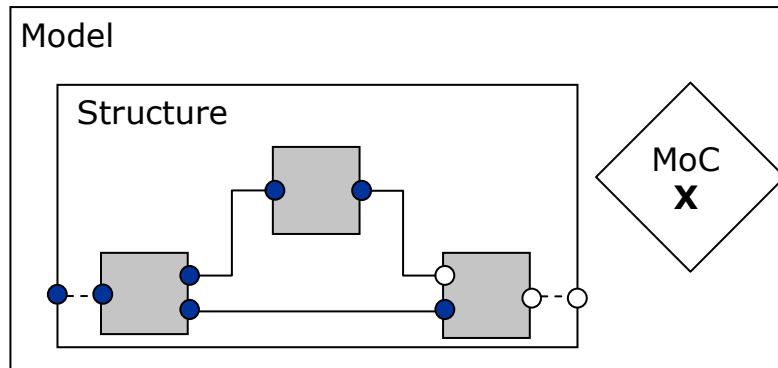
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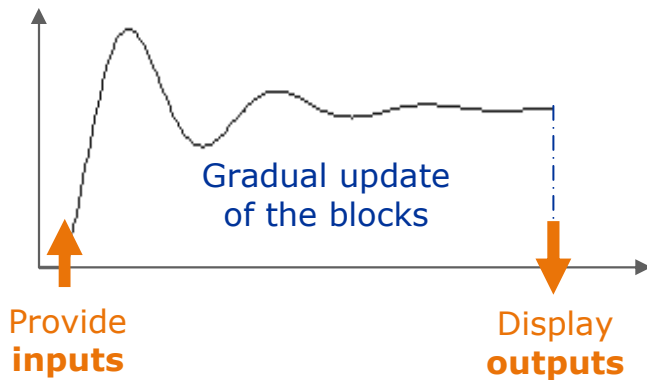
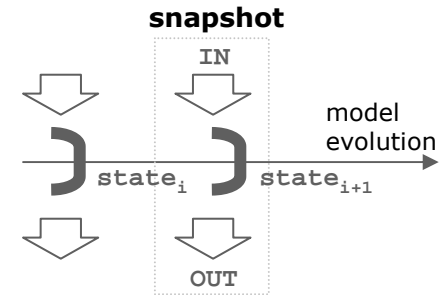


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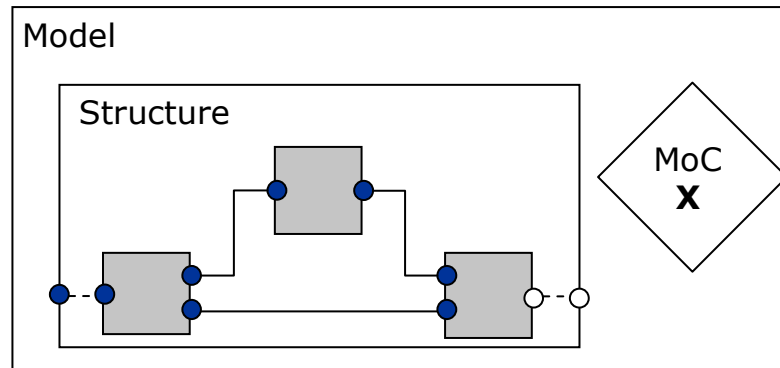
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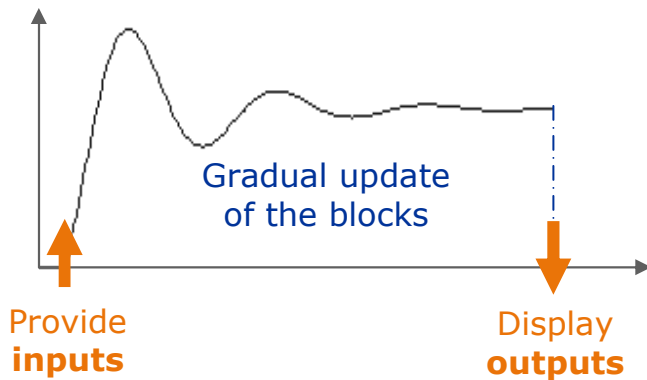
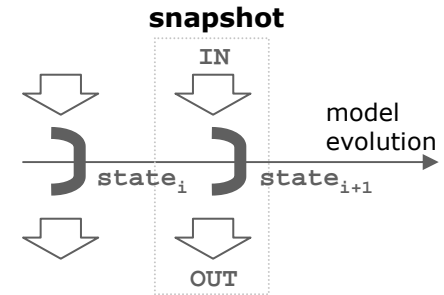


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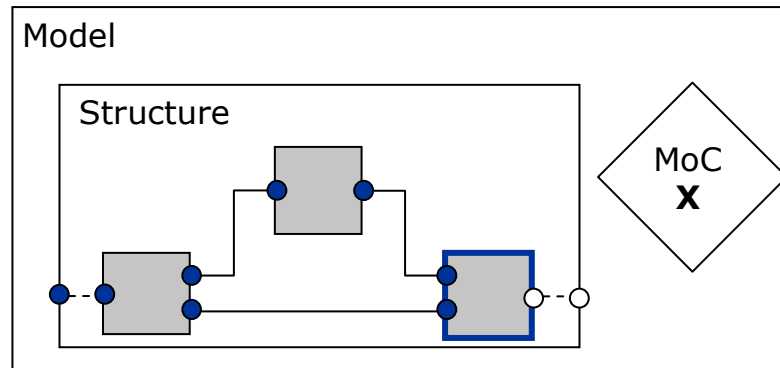
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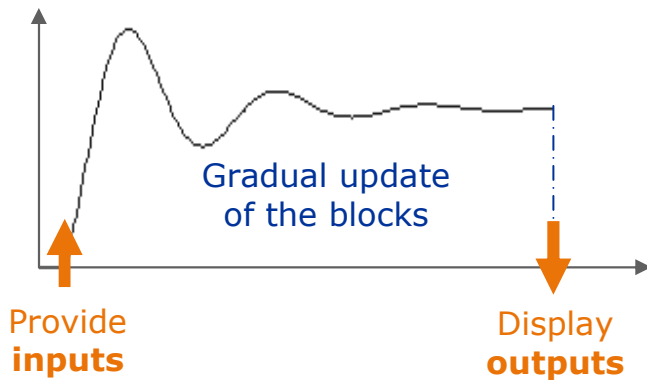
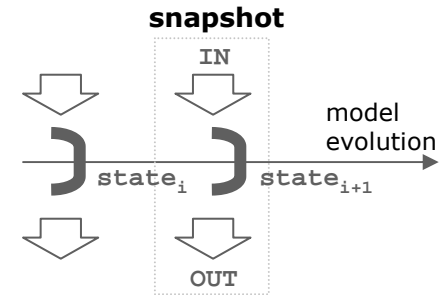


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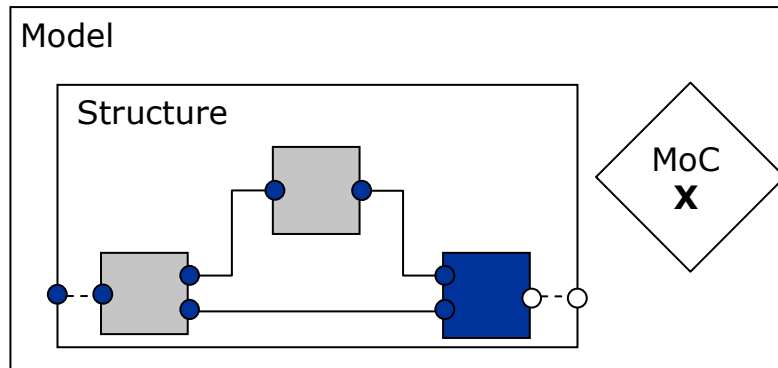
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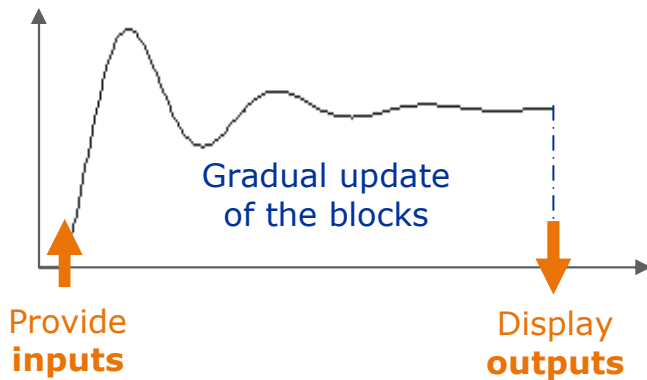
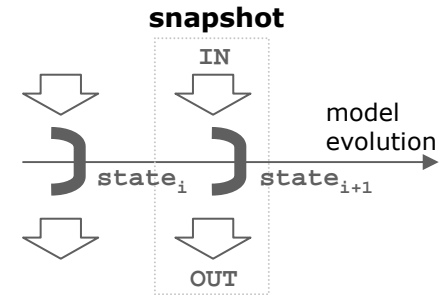


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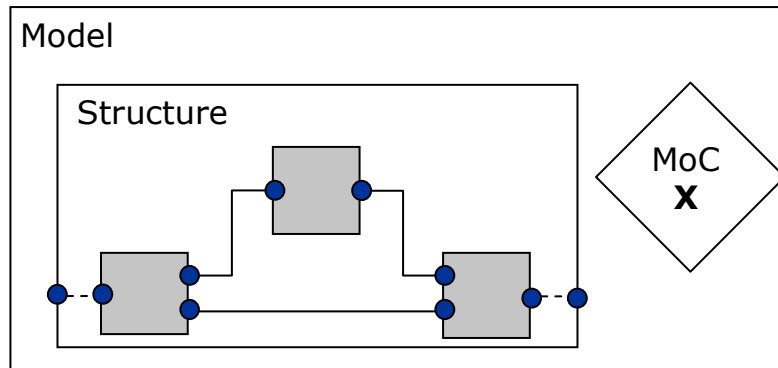
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■ Example

After update

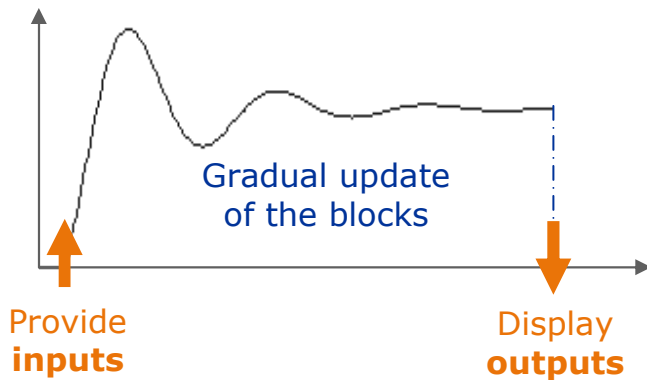
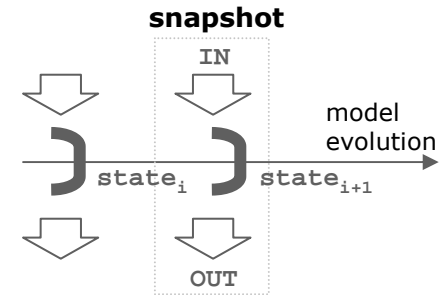


Executing an heterogeneous model

■ One **execution** =

- ▶ A sequence of **successive snapshots** of the model

■ One **snapshot** =



▶ Causal execution

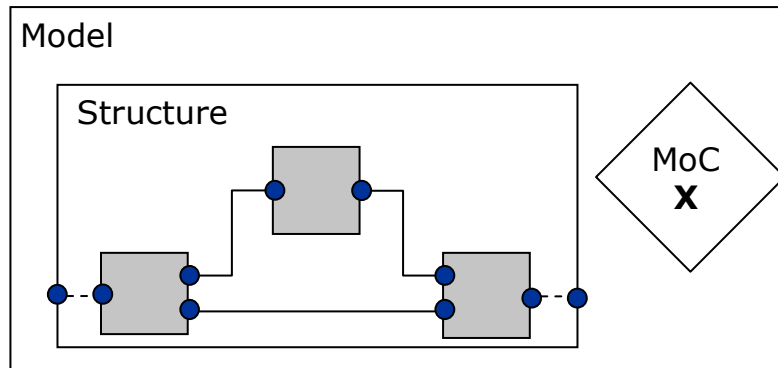
- $\text{State}_i + \text{inputs}_i \rightarrow \text{outputs}_i + \text{State}_{i+1}$

▶ Gradual update of the model blocks

- **Schedule** of the block to update
- **Update** of the block
- **Propagation** of the produced data

■ Example

Display outputs

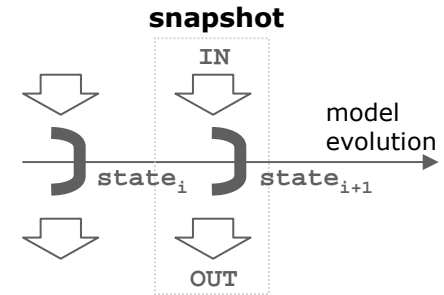


All the outputs are known
→ the snapshot is determined

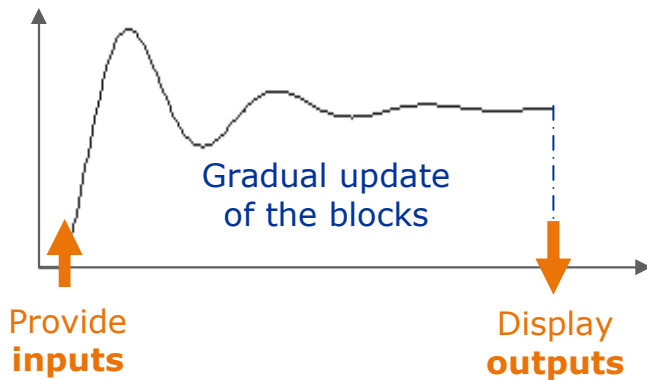
Executing an heterogeneous model

■ One **execution** =

- ▶ A sequence of **successive snapshots** of the model



■ One **snapshot** =



▶ Causal execution

- $\text{State}_i + \text{inputs}_i \rightarrow \text{outputs}_i + \text{State}_{i+1}$

▶ Gradual update of the model blocks

- **Schedule** of the block to update
- **Update** of the block
- **Propagation** of the produced data

■ Generic **execution algorithm**

- ▶ A set of **generic operations**
- ▶ **Semantics specified** using our language
- ▶ **Hierarchical execution**
 - InterfaceBlocks have **special operations** in order to adapt the semantics between MoCs



Intended workflow & needed effort

ONCE !

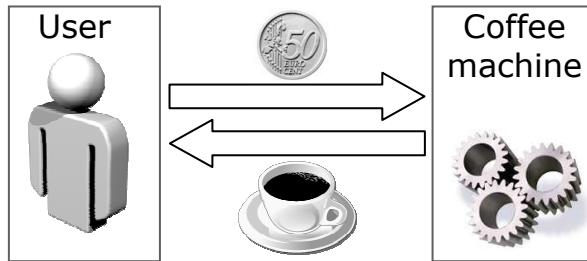
1. An expert of a modeling language describes
 - ▶ The structural and semantic elements of the language
 - Specialized meta-model
 - Imperative semantics of the MoC
 - ▶ Transformations from the original meta-model of the language to the ModHel'X meta-model for maximizing the reuse of existing models
2. Experts define interaction patterns for each pair of model of computation that may interact
 - ▶ Interaction pattern = “classical glue”
 - ▶ Parameters allow the designers to fine tune the adaptation
3. Designers use ModHel'X

- Conclusion: **ModHel'X is a generic and modular framework for executing heterogeneous models** with
 - A **generic meta-model** for representing heterogeneous models
 - A **generic algorithm** for executing heterogeneous models
 - A **language** for specifying the semantics of models of computations and of their interactions
 - ▶ Applications: (joint) simulation, code generation, etc.
- Work in progress
 - ▶ Prototype based on the Eclipse Modeling Framework (EMF)
 - Several implemented MoCs
 - ▶ **Concrete syntax** of our language (OMG ImperativeOCL – QVT)
 - ▶ **Formal semantics** of our algorithm and language
- Perspectives
 - ▶ Facets (non-functional properties for embedded systems)
 - ▶ Model refinement & symbolic execution

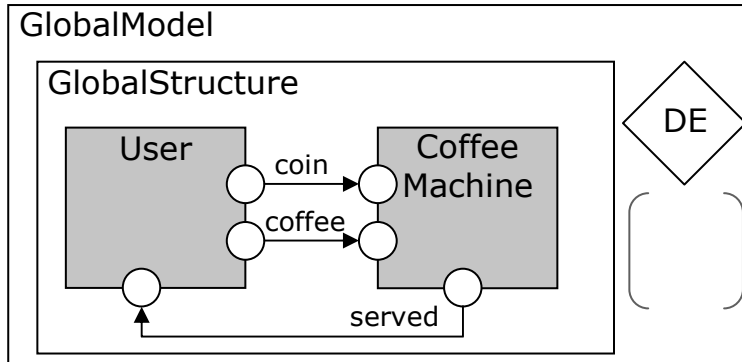
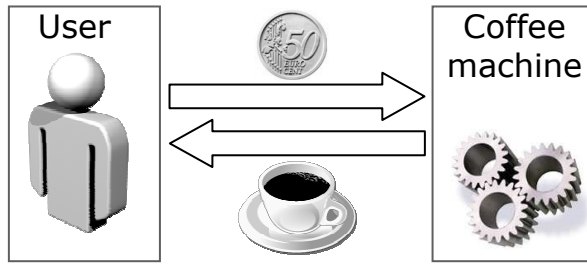
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- **[Kong03]** C. Kong and P. Alexander. The Rosetta meta-model framework. In Proceedings of the IEEE Engineering of Computer-Based Systems Symposium and Workshop (ECBS'03), april 2003

Appendix

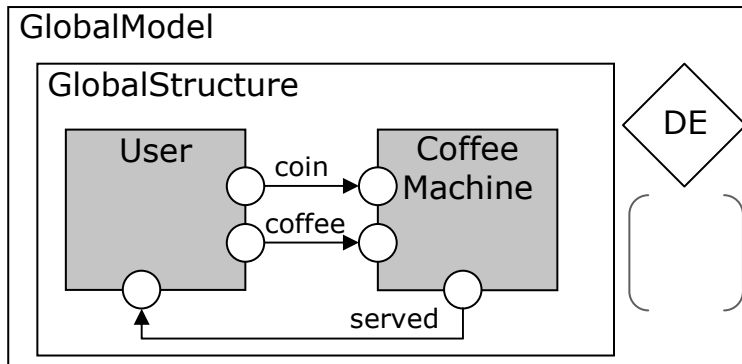
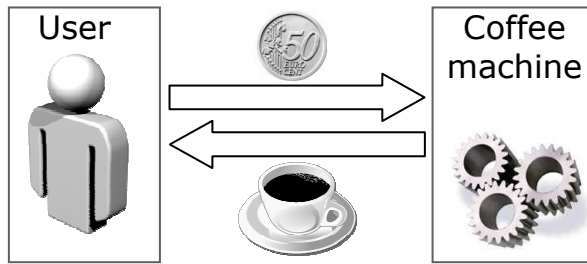
The coffee machine example



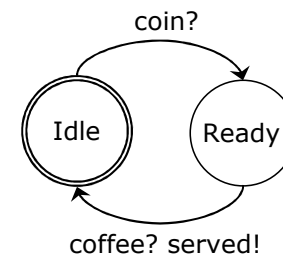
The coffee machine example



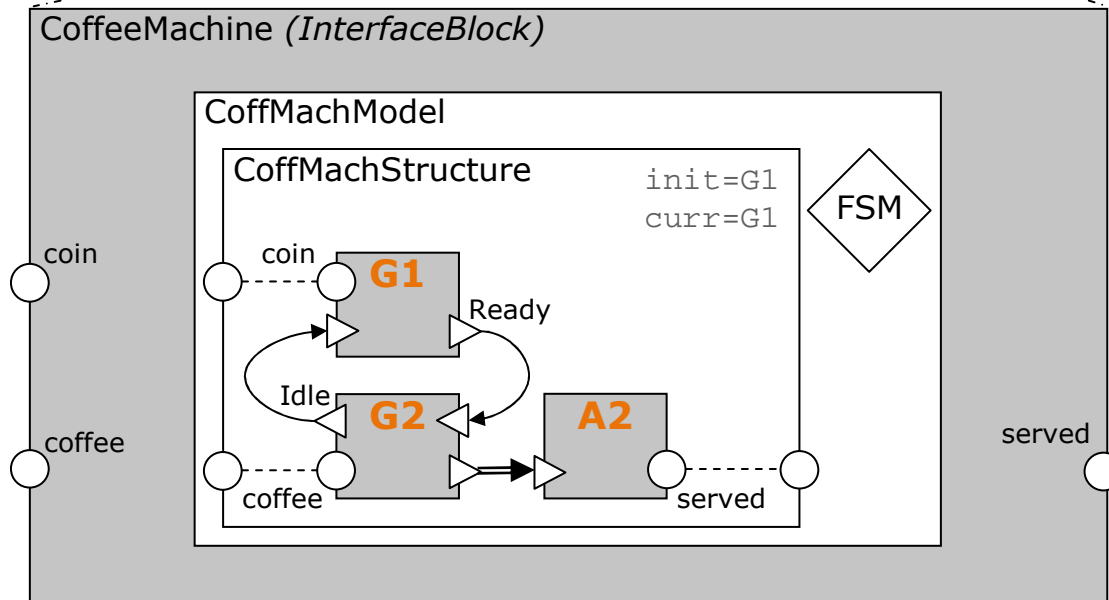
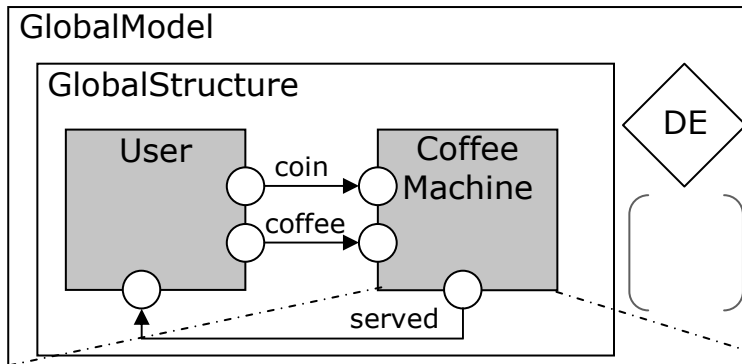
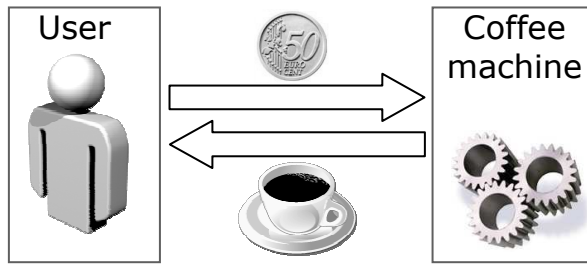
The coffee machine example



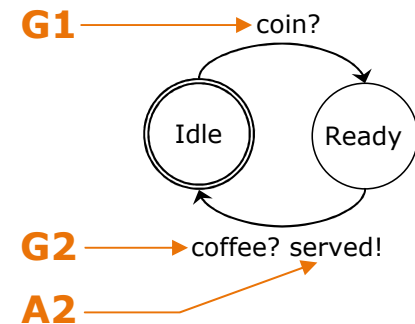
■ Coffee machine automaton



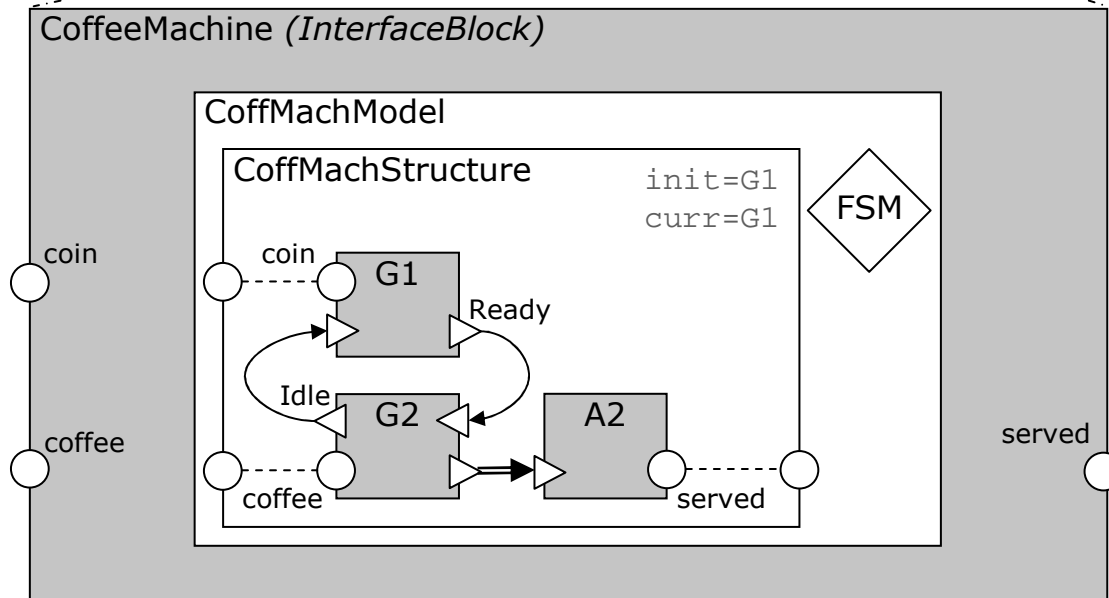
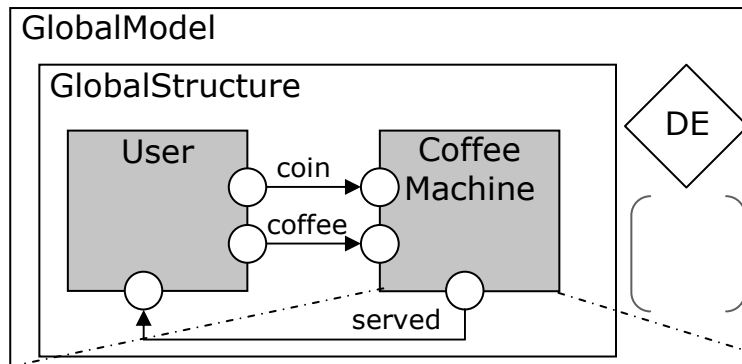
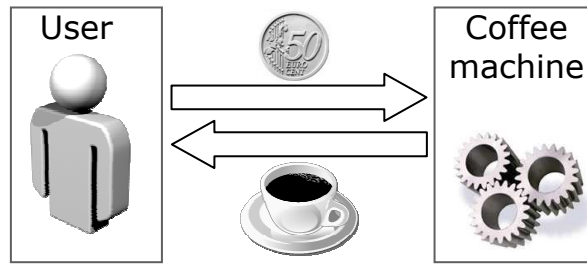
The coffee machine example



■ Coffee machine automaton

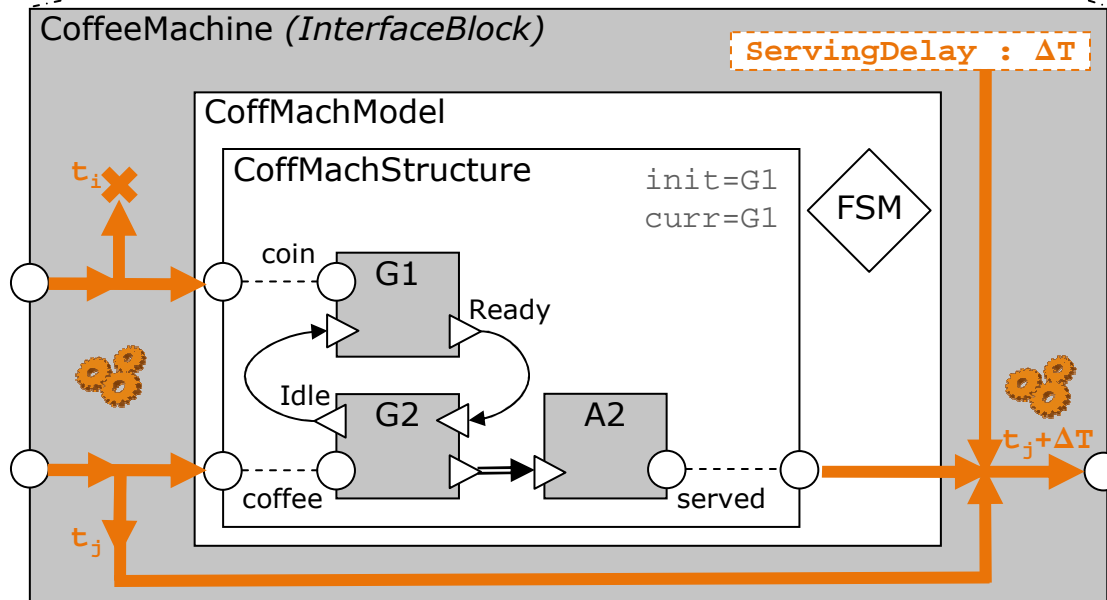
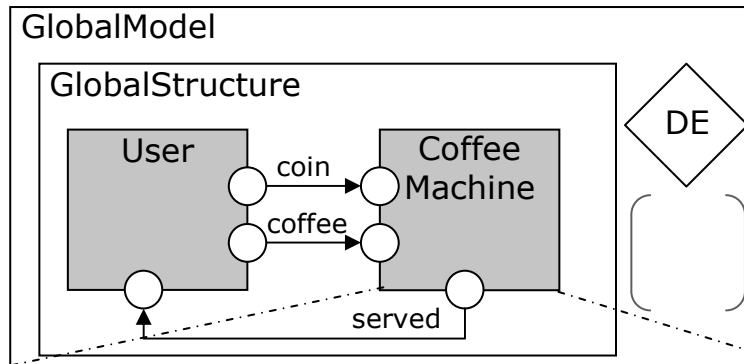
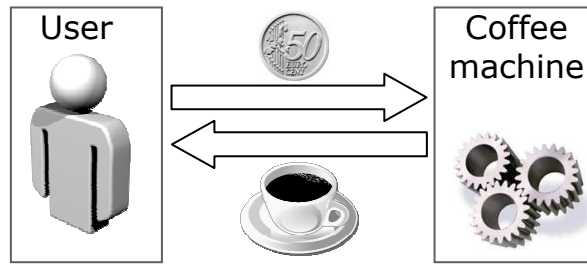


The coffee machine example



- Time “gluing” ?
- Serving delay ?

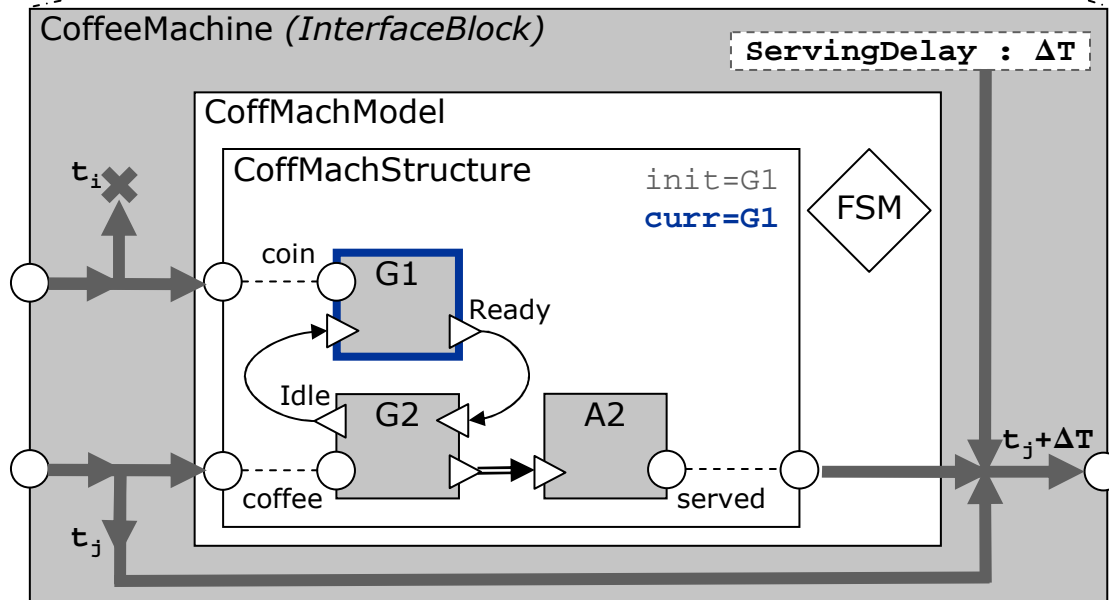
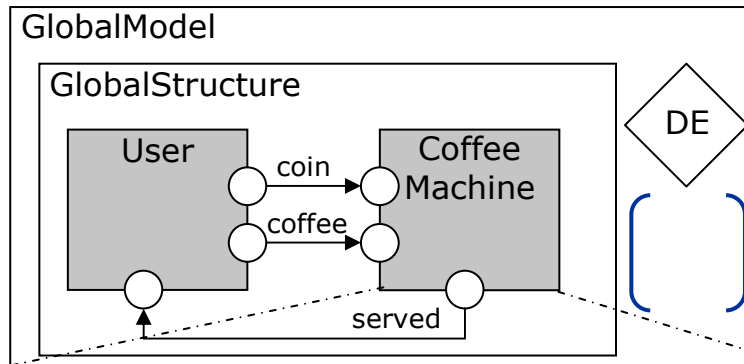
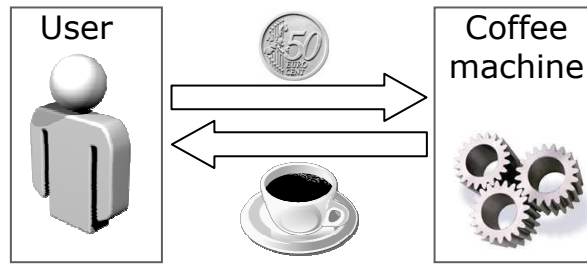
The coffee machine example



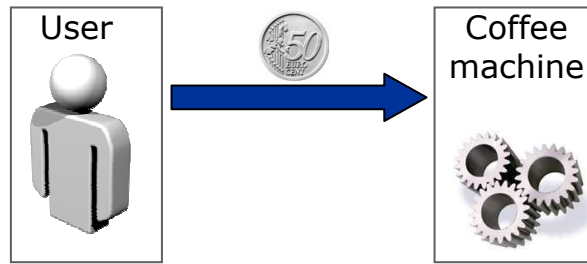
- Time “gluing” ?
Serving delay ?

- ▶ adaptIn
- ▶ adaptOut

Running the model

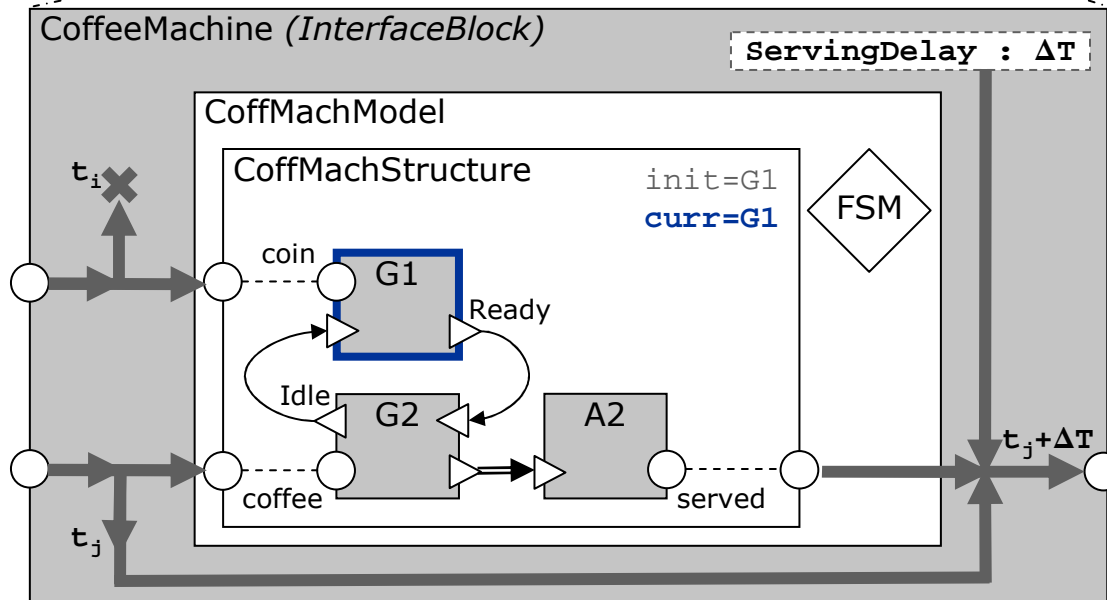
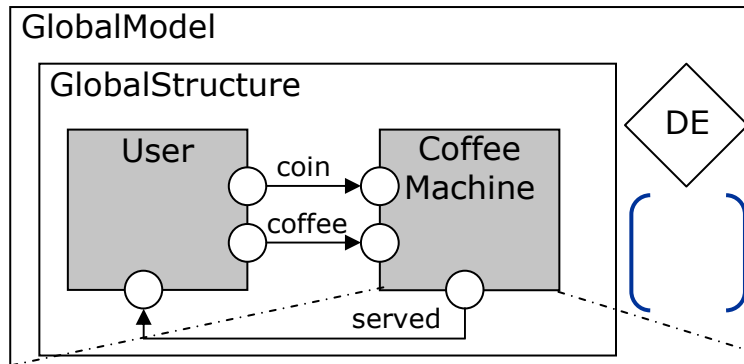


Running the model

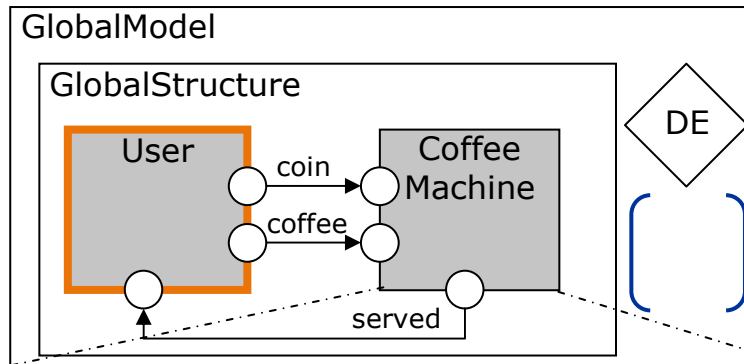
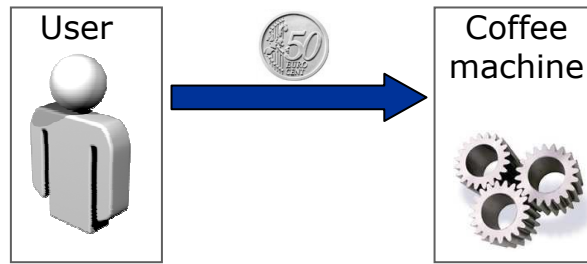


■ **Constraint** on the user

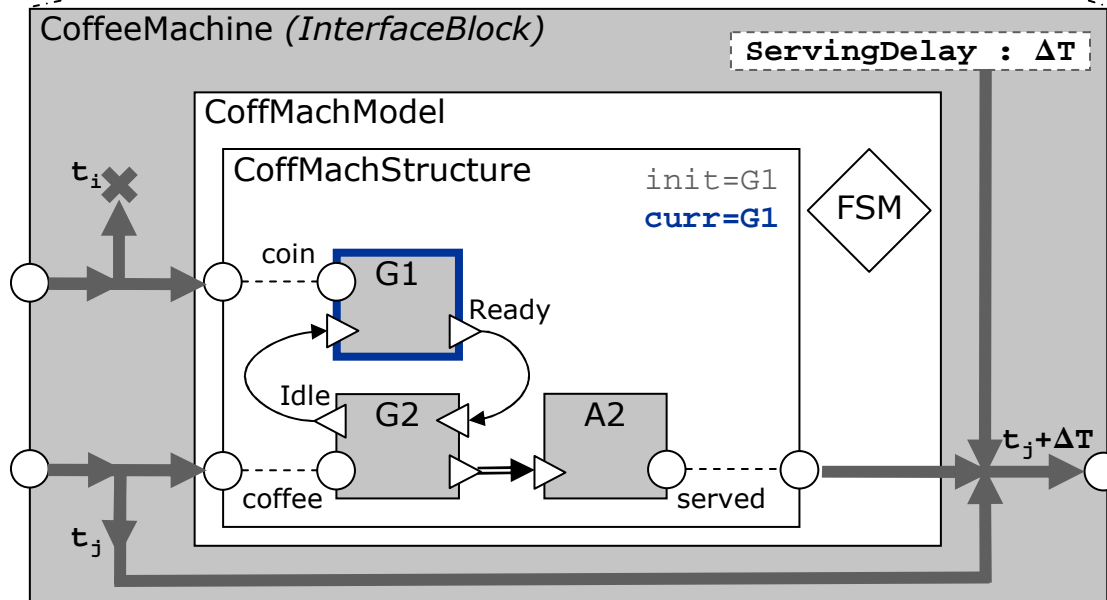
constraints=
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Running the model



constraints=
[user,0]

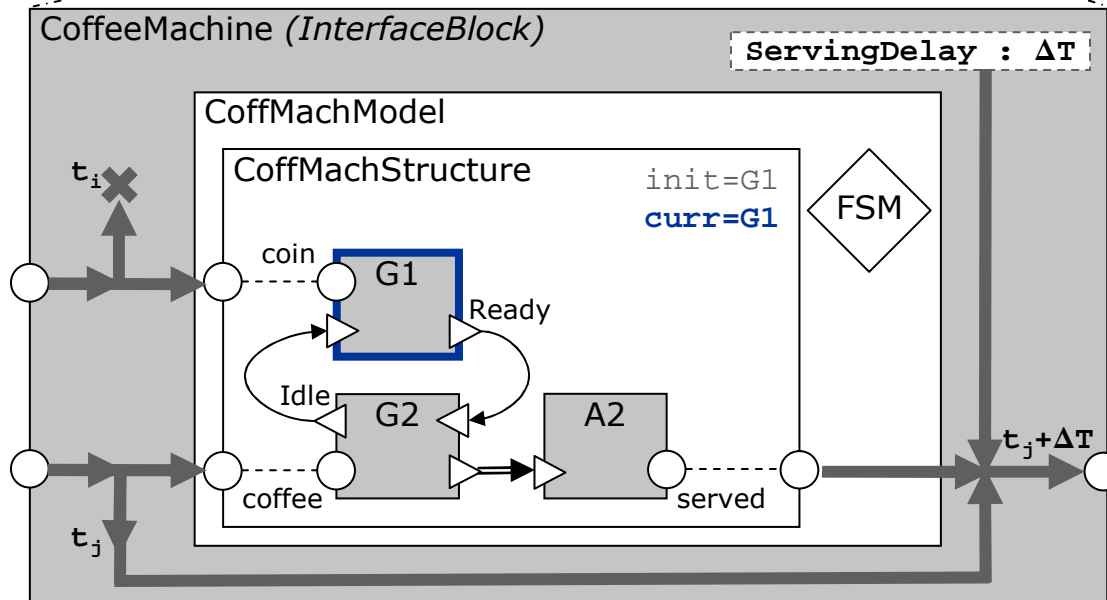
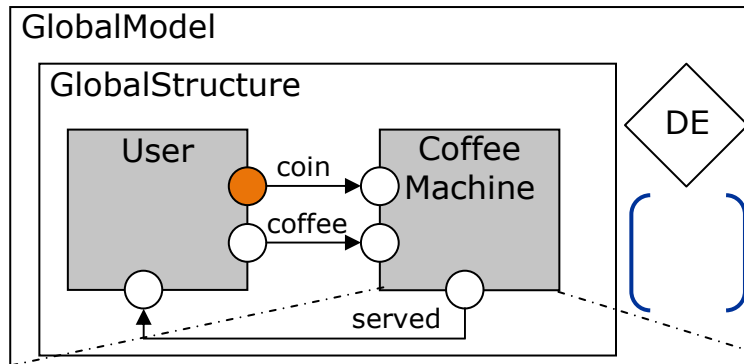
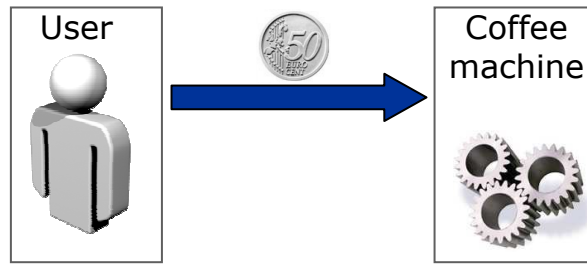


■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

Running the model

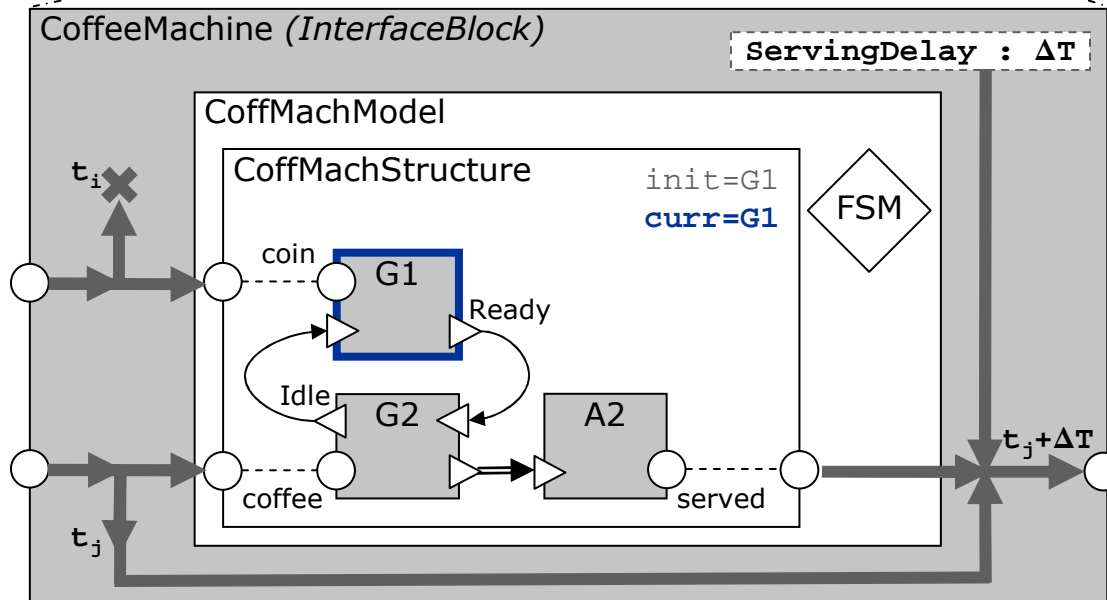
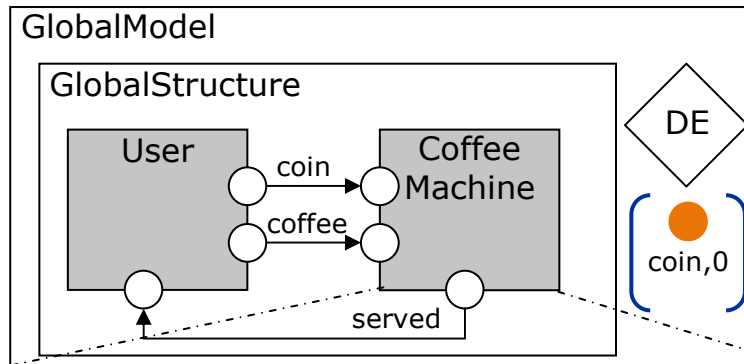
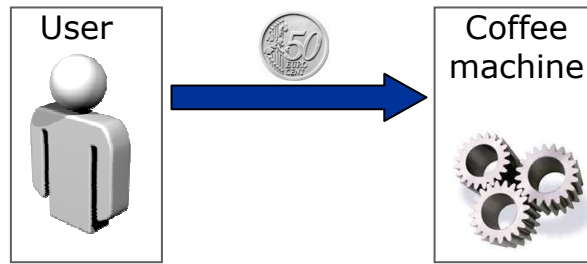


■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

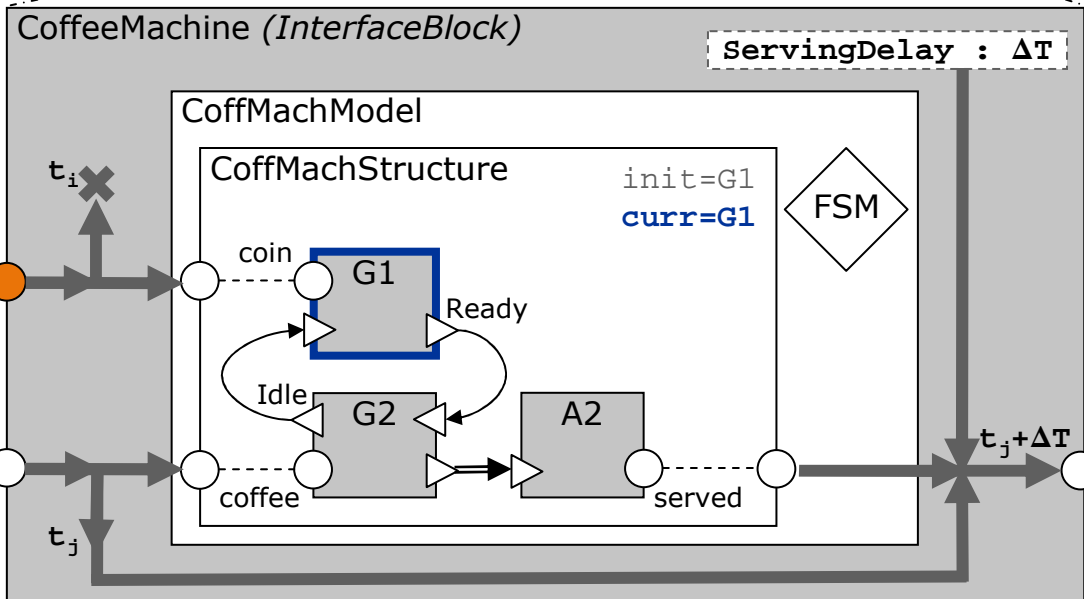
Running the model



■ **Constraint** on the user

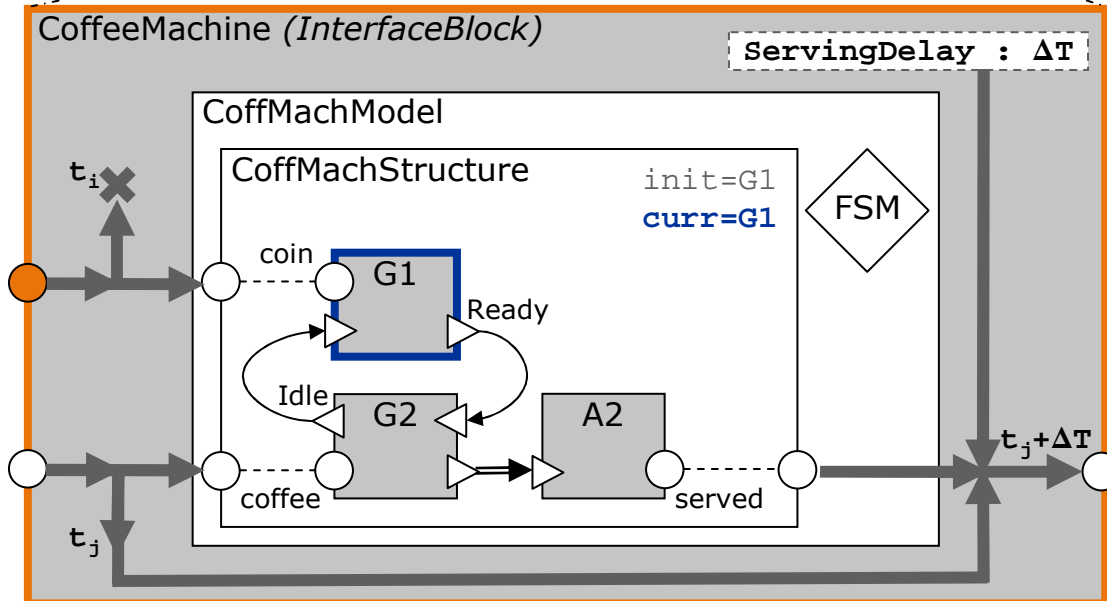
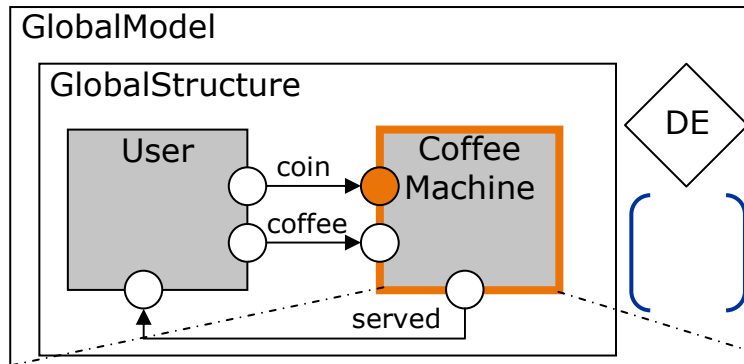
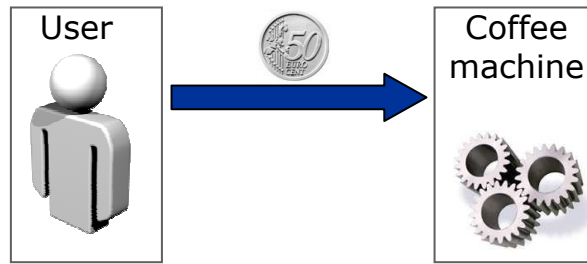
■ **First snapshot**

▶ $t_{DE} = 0$



- **Constraint** on the user
- **First snapshot**
 - ▶ $t_{DE} = 0$
“the user inserts the coin”

Running the model



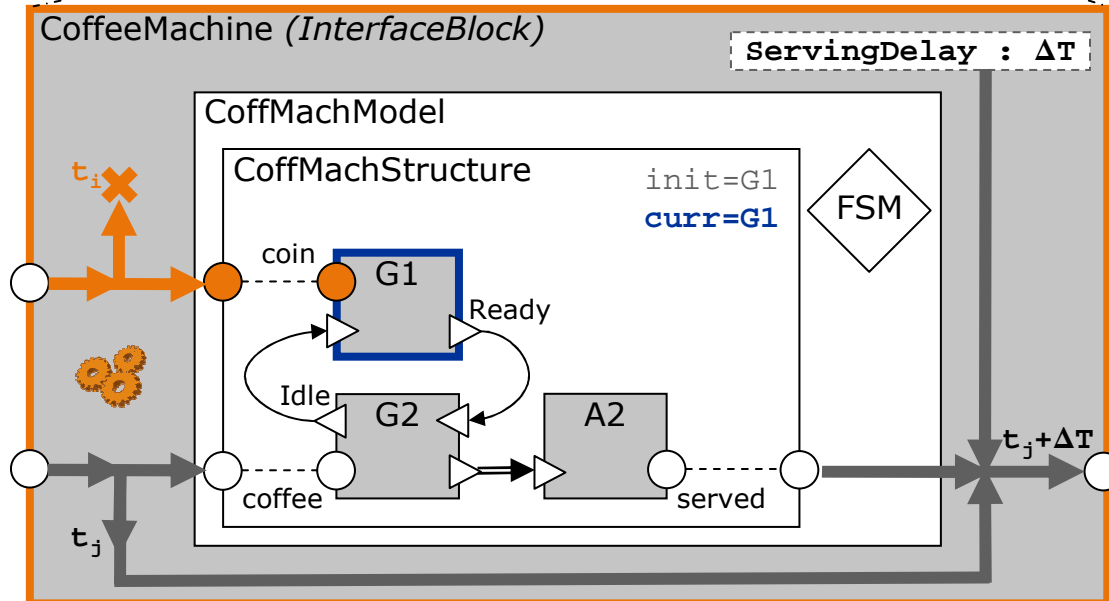
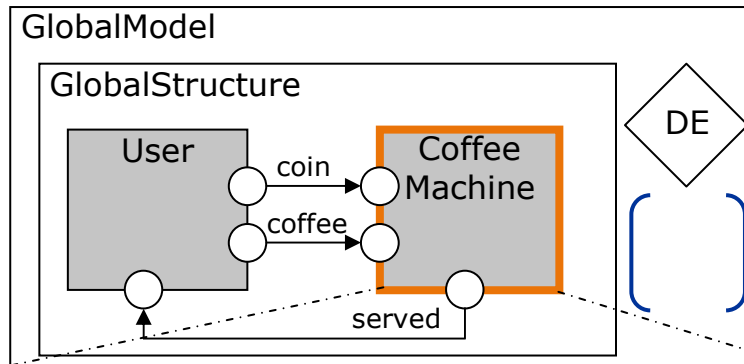
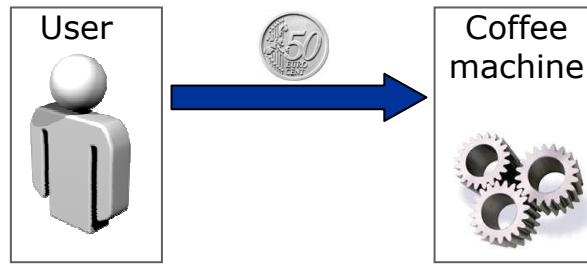
■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

“the user inserts the coin”

Running the model



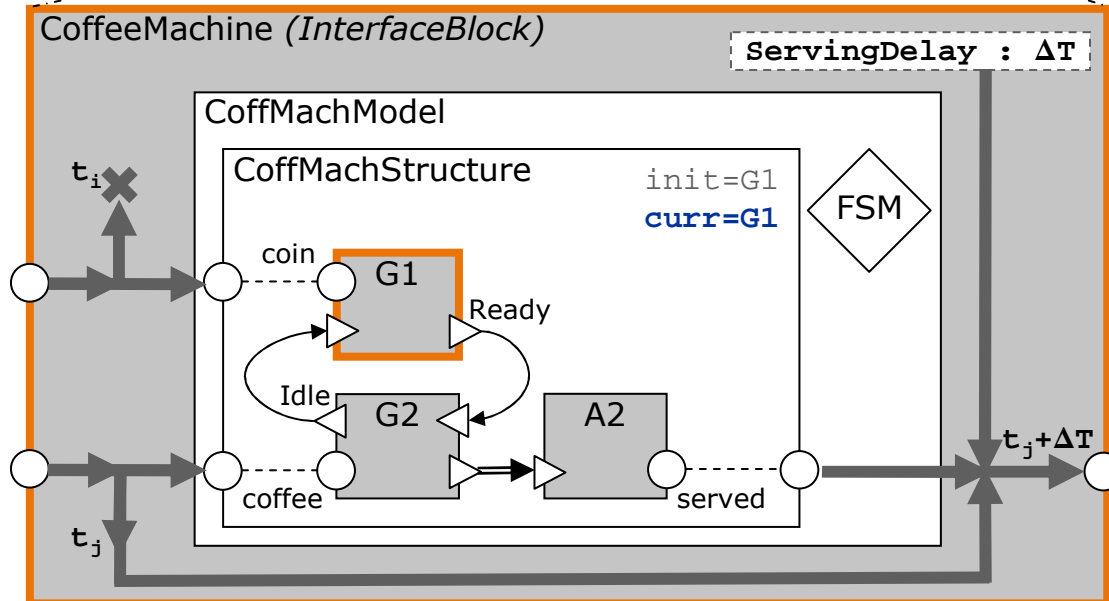
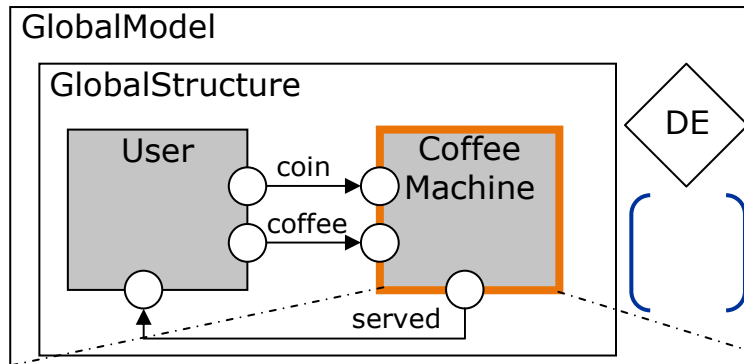
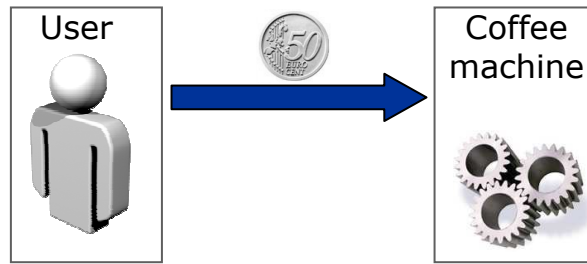
■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

“the user inserts the coin”

Running the model



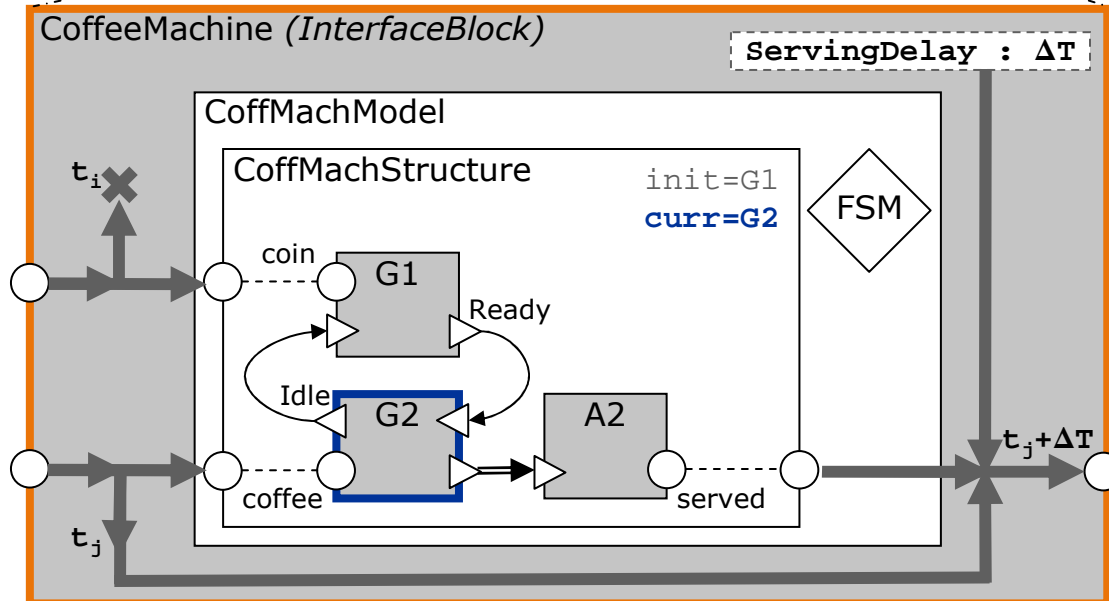
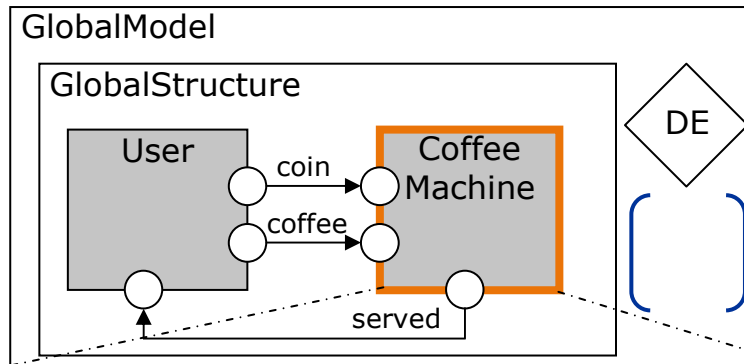
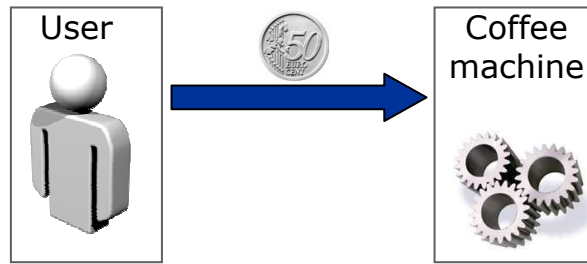
■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

“the user inserts the coin”

Running the model



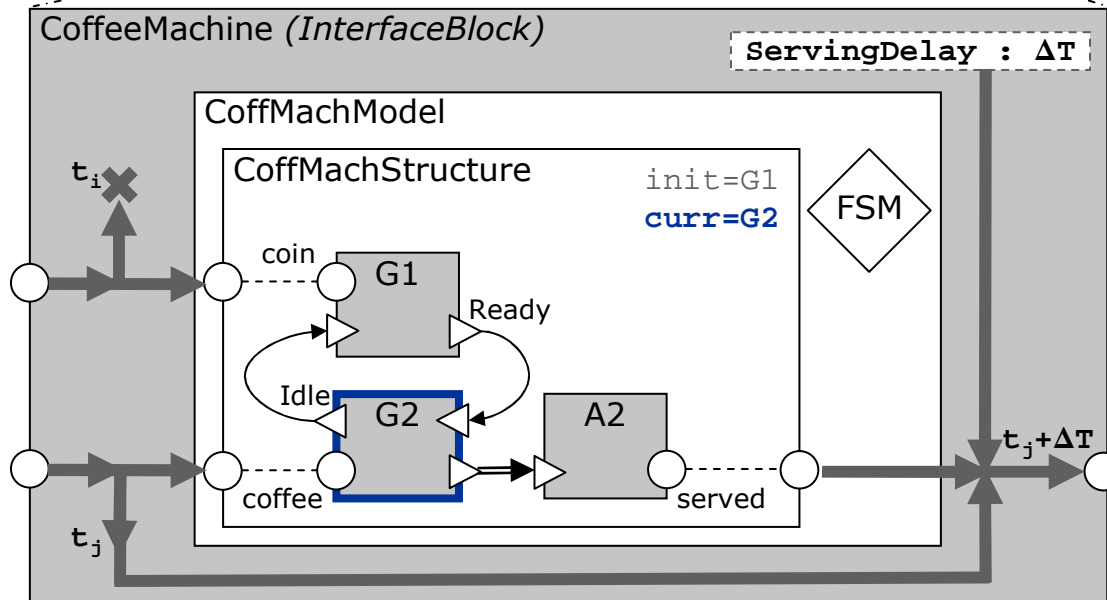
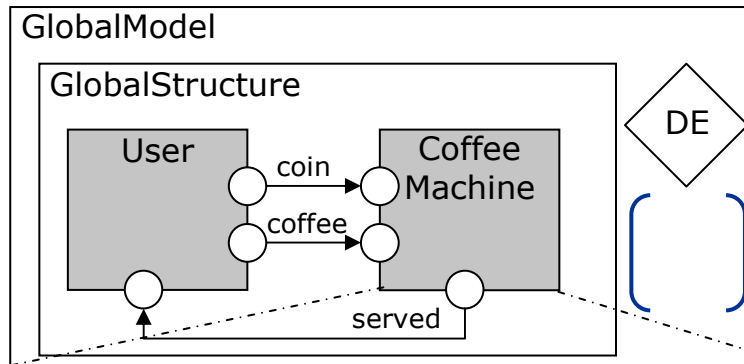
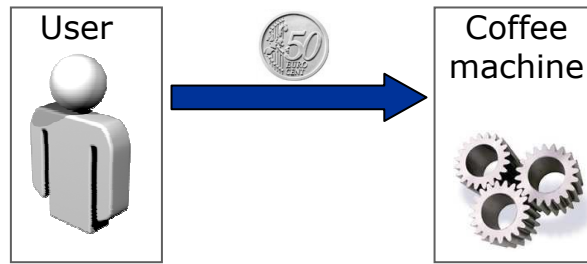
■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

“the user inserts the coin”

Running the model



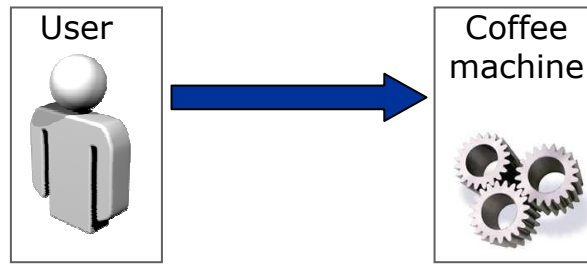
■ **Constraint** on the user

■ **First snapshot**

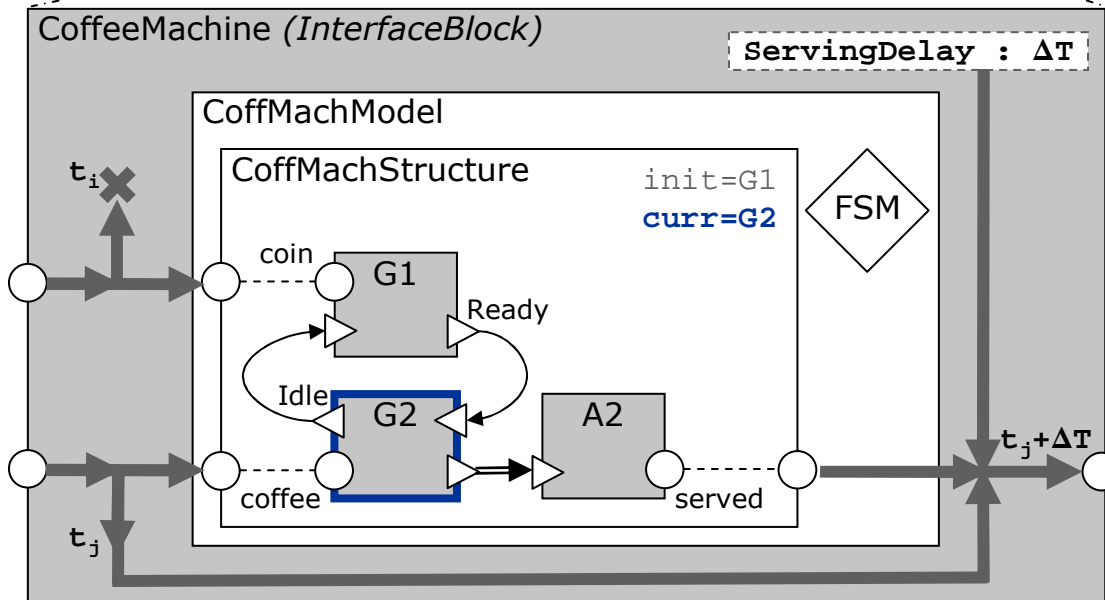
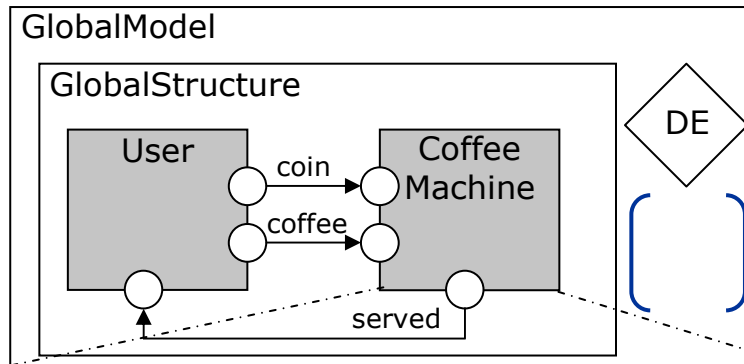
▶ $t_{DE} = 0$

“the user inserts the coin”

Running the model



constraints=
[user, T_{user}]



■ **Constraint** on the user

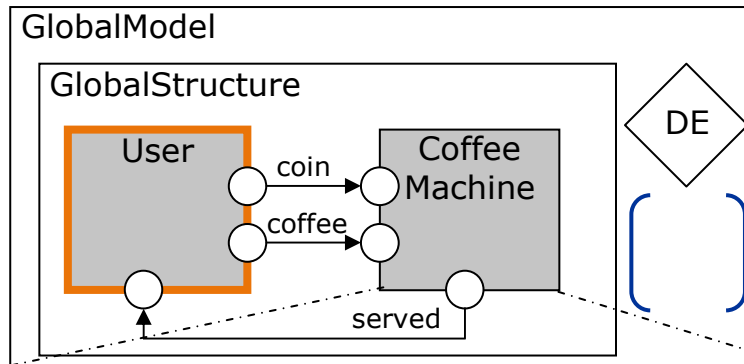
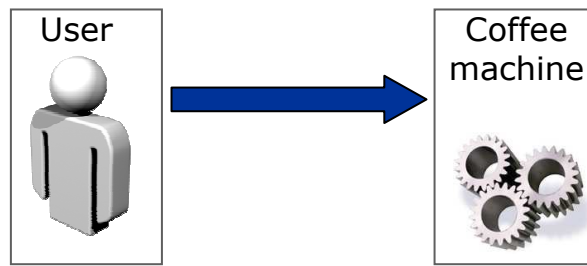
■ **First snapshot**

▶ $t_{DE} = 0$

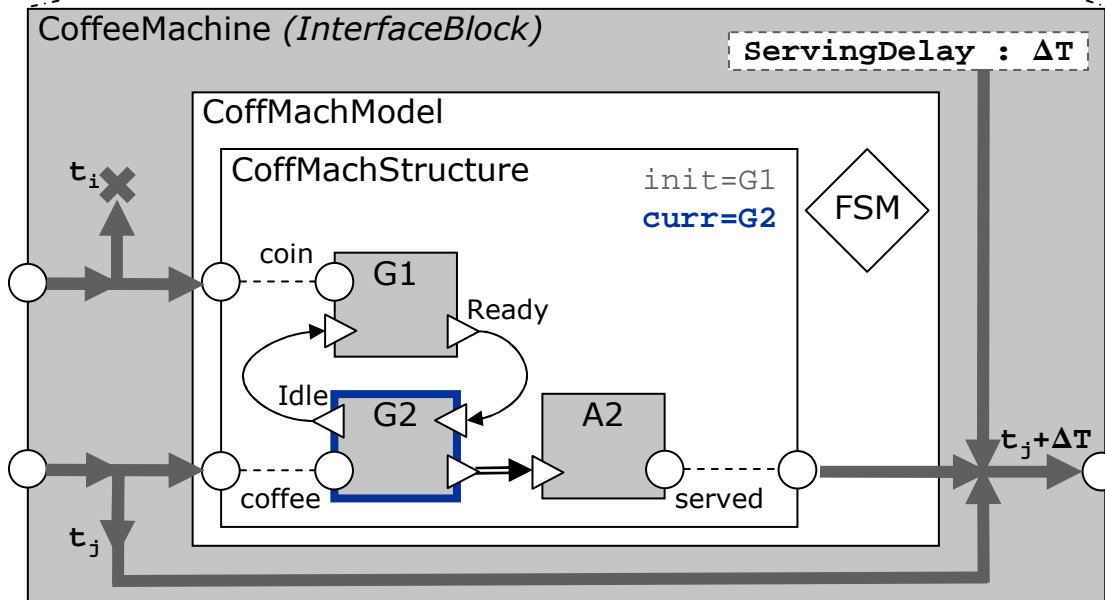
“the user inserts the coin”

▶ **Constraint** on the user

Running the model



constraints=
[user, T_{user}]



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

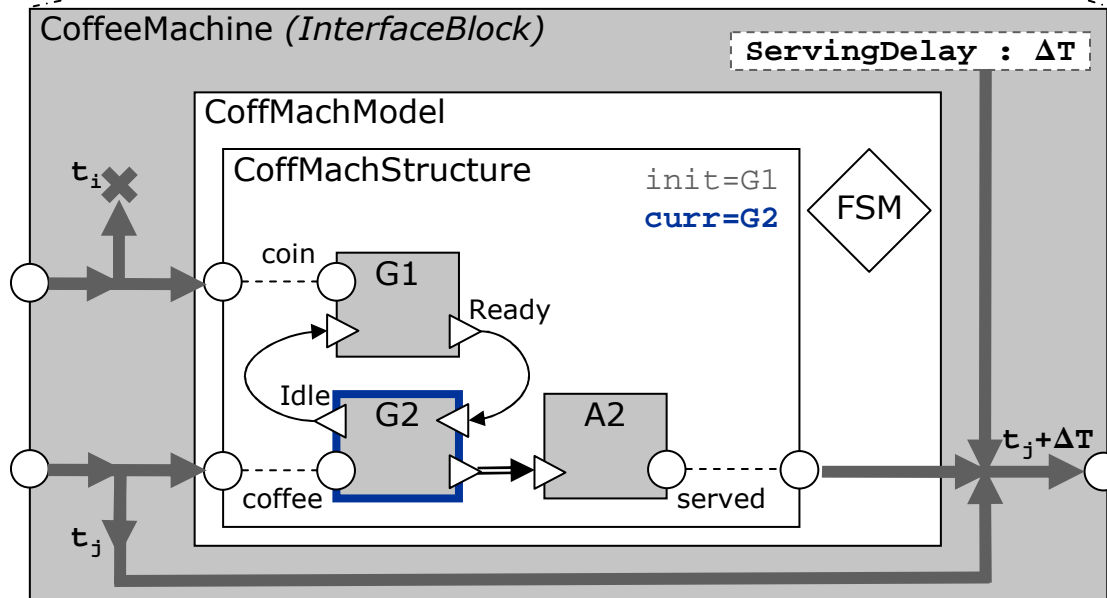
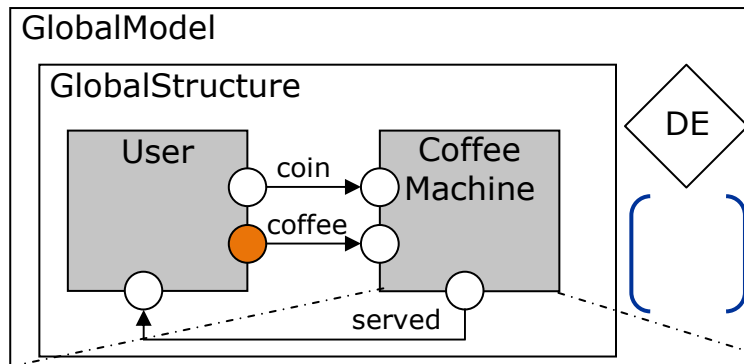
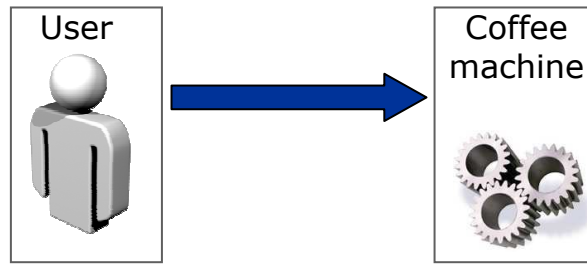
“the user inserts the coin”

▶ Constraint on the user

■ Second snapshot

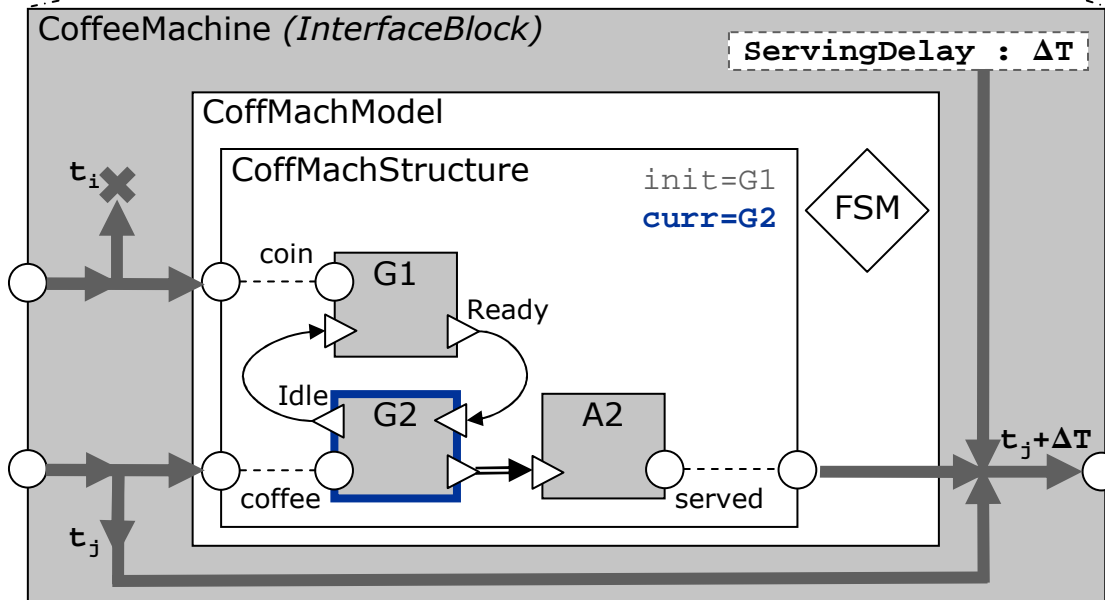
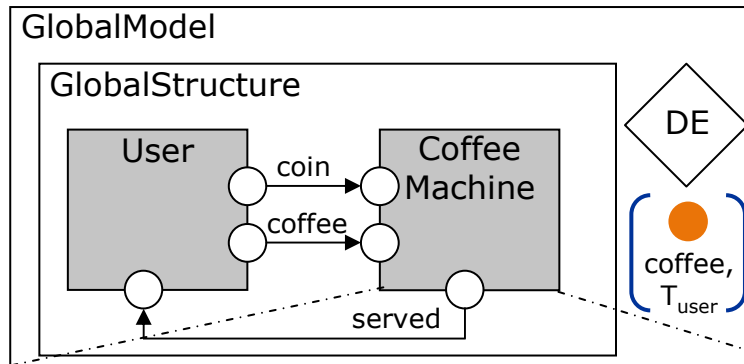
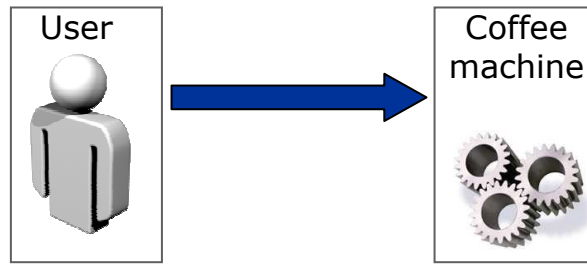
▶ $t'_{DE} = T_{user}$

Running the model



- **Constraint** on the user
- **First snapshot**
 - ▶ $t_{DE} = 0$
 - “the user inserts the coin”
 - ▶ **Constraint** on the user
- **Second snapshot**
 - ▶ $t'_{DE} = T_{user}$

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

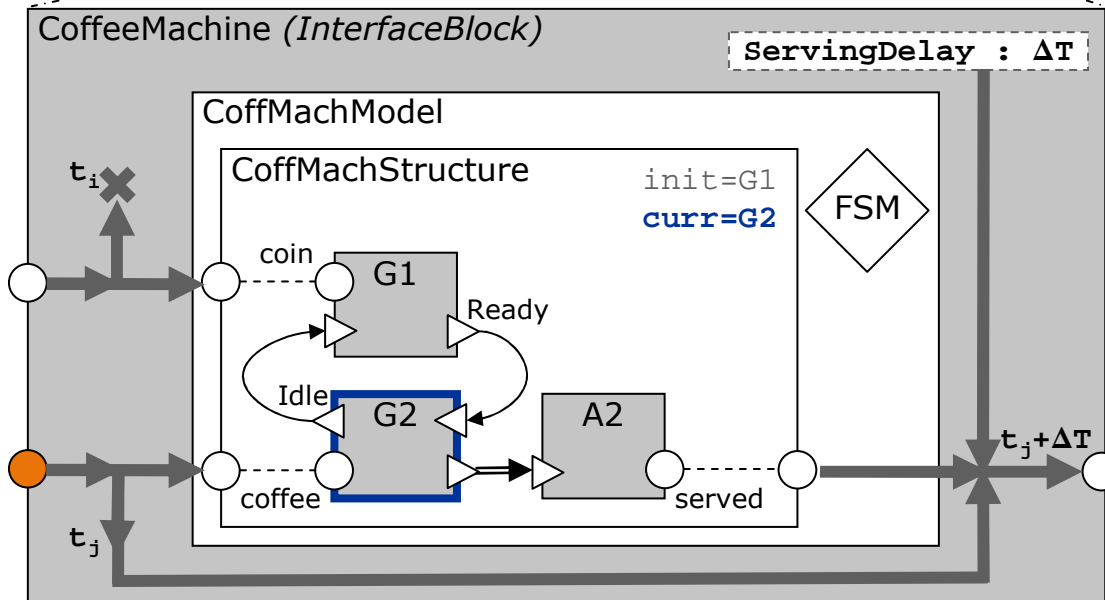
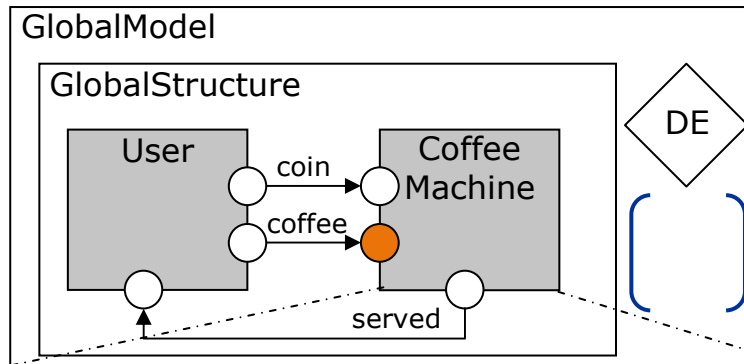
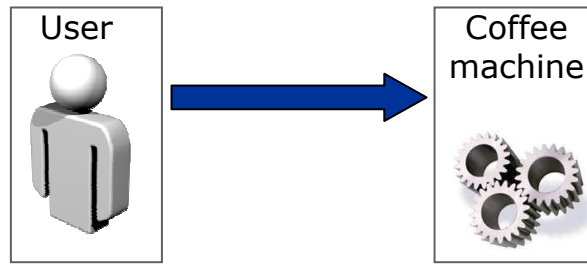
“the user inserts the coin”

▶ Constraint on the user

■ Second snapshot

▶ $t'_{DE} = T_{user}$

Running the model



■ Constraint on the user

■ First snapshot

► $t_{DE} = 0$

“the user inserts the coin”

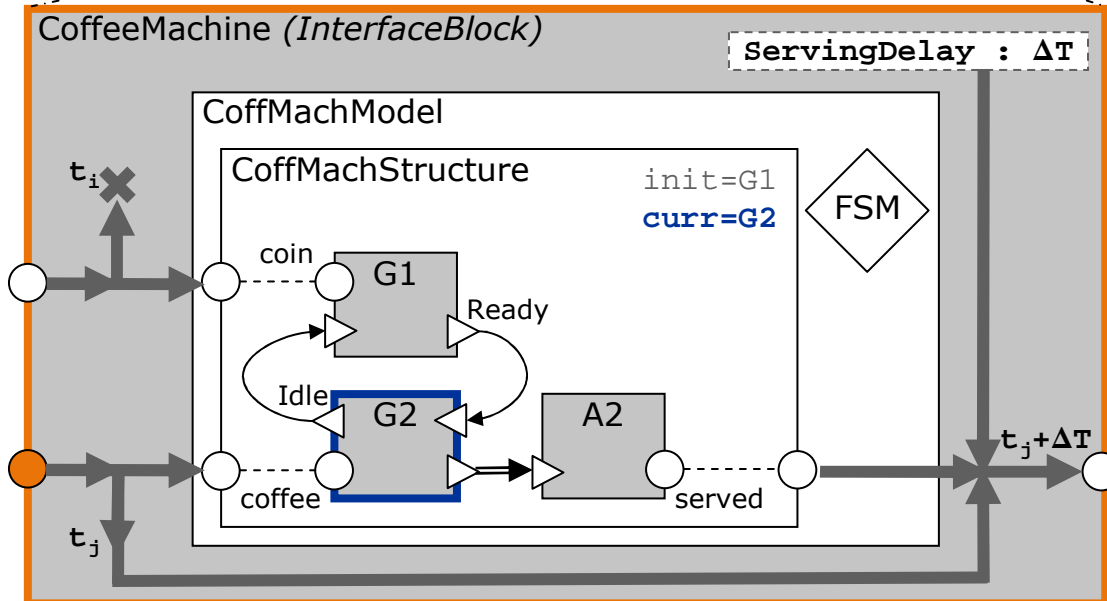
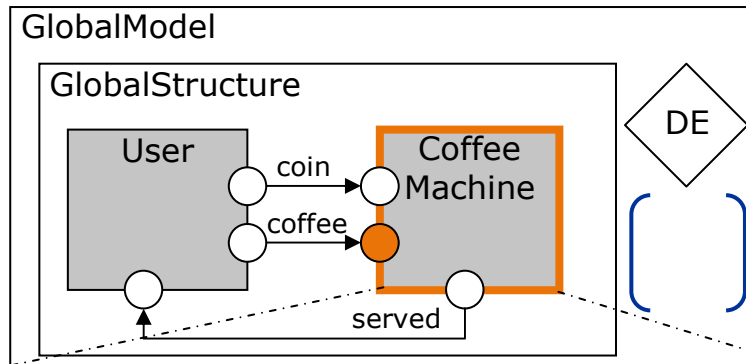
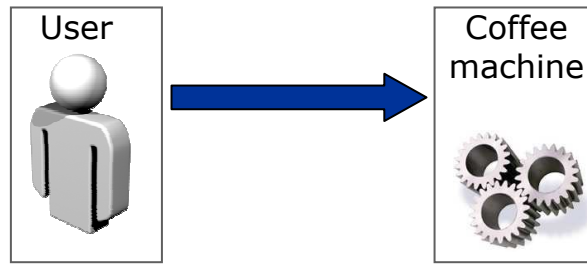
► Constraint on the user

■ Second snapshot

► $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

“the user inserts the coin”

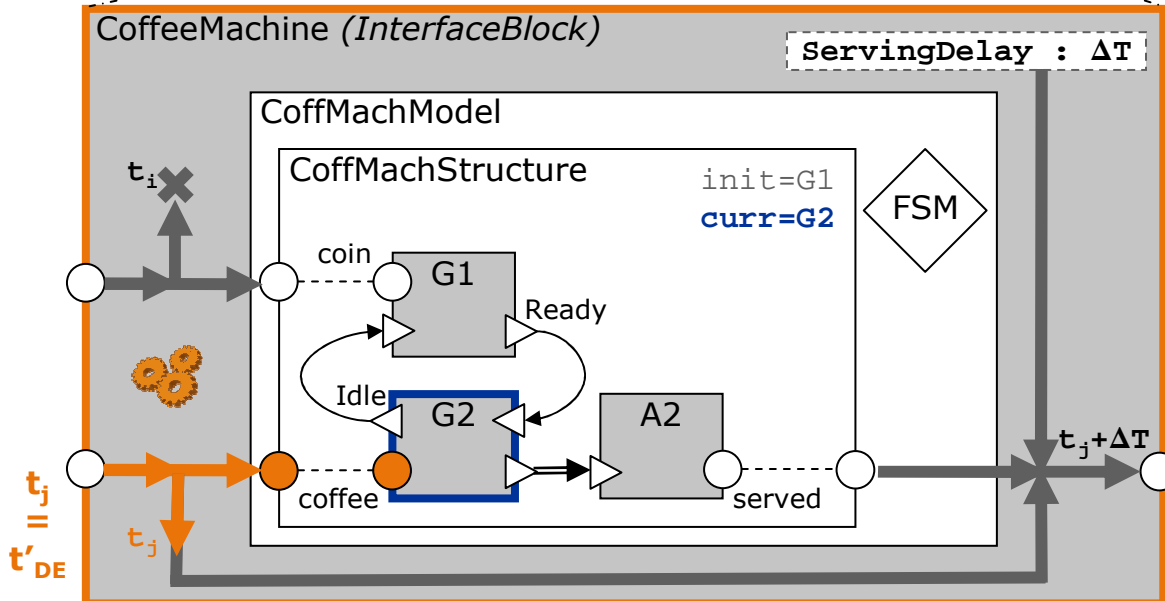
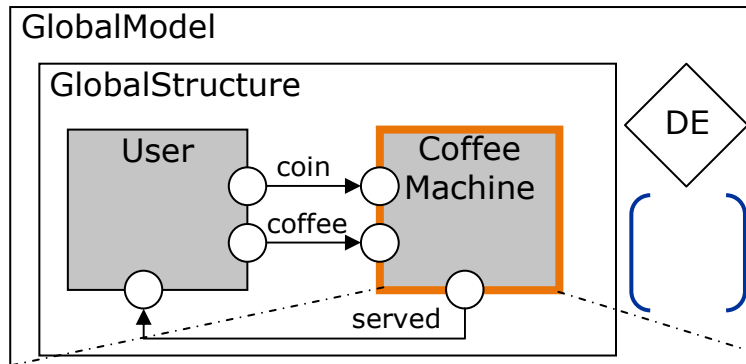
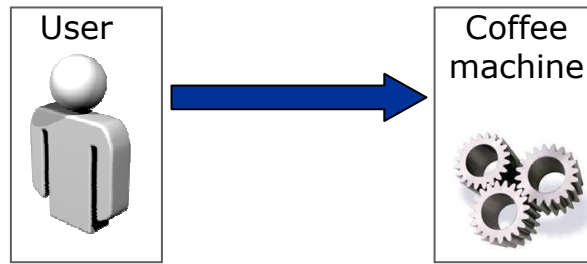
▶ Constraint on the user

■ Second snapshot

▶ $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

► $t_{DE} = 0$

“the user inserts the coin”

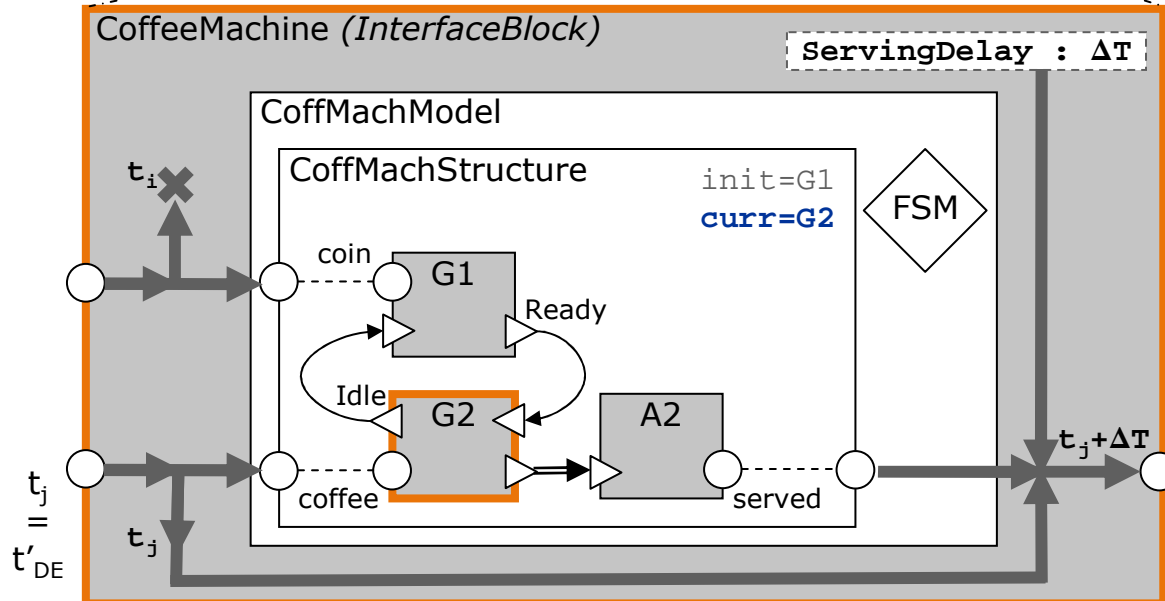
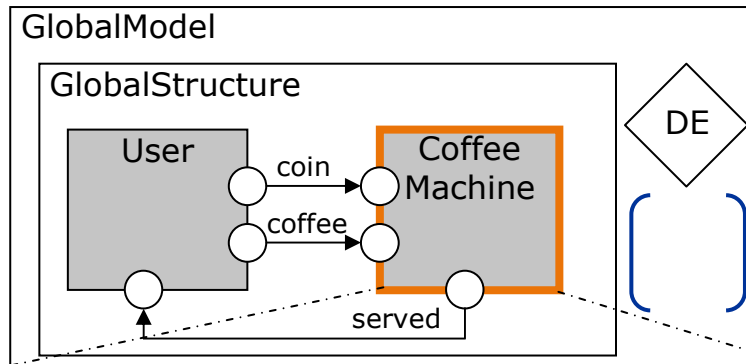
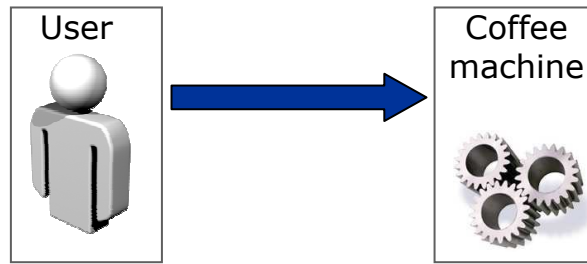
► Constraint on the user

■ Second snapshot

► $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

► $t_{DE} = 0$

“the user inserts the coin”

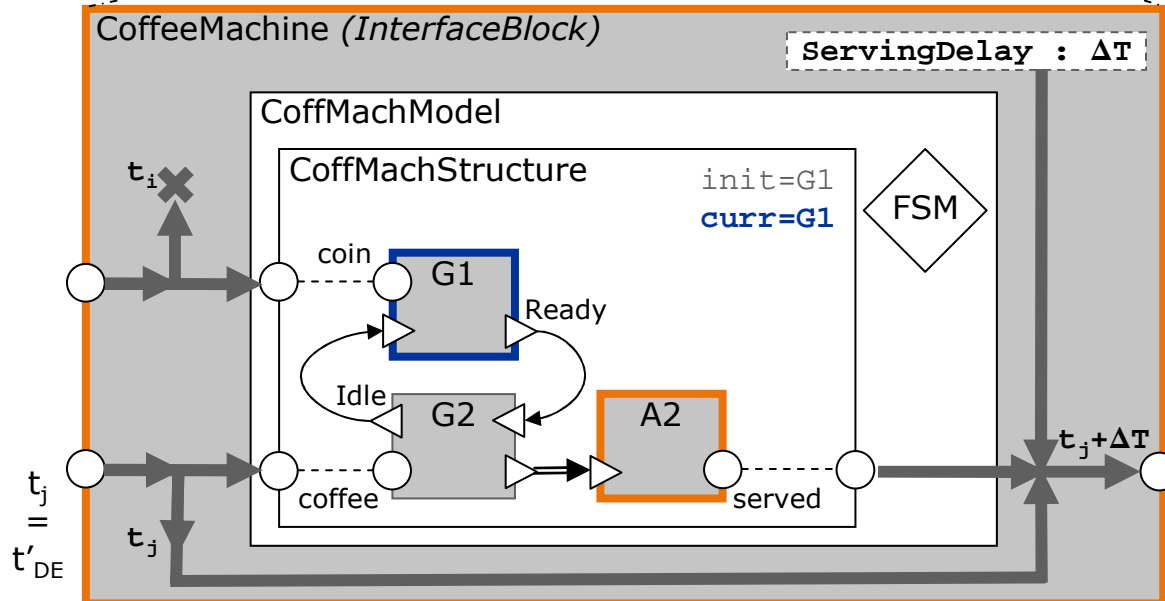
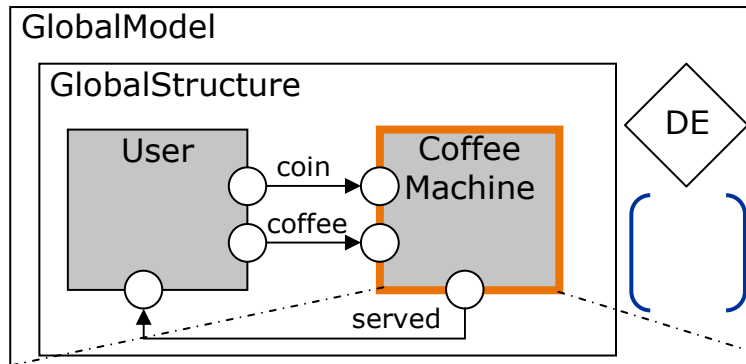
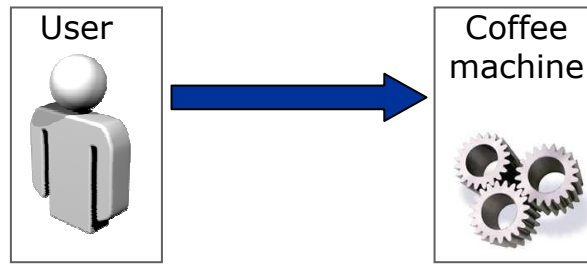
► Constraint on the user

■ Second snapshot

► $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

► $t_{DE} = 0$

“the user inserts the coin”

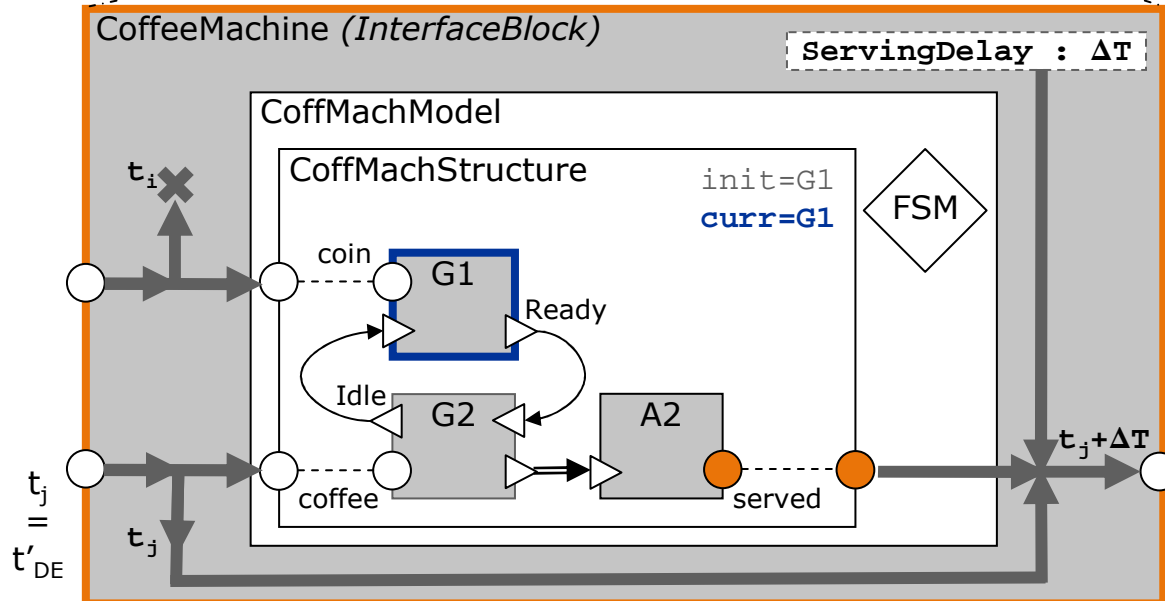
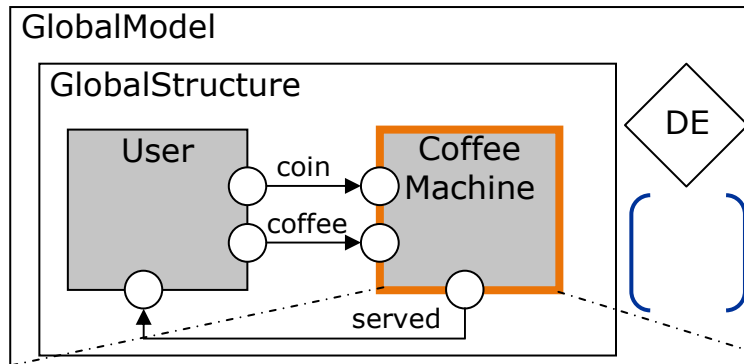
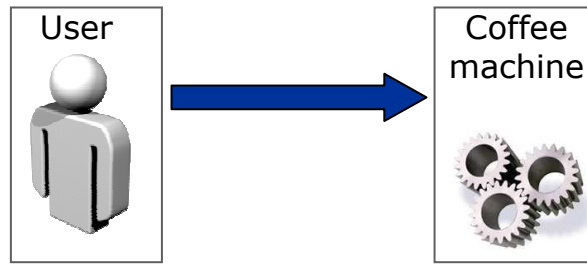
► Constraint on the user

■ Second snapshot

► $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

“the user inserts the coin”

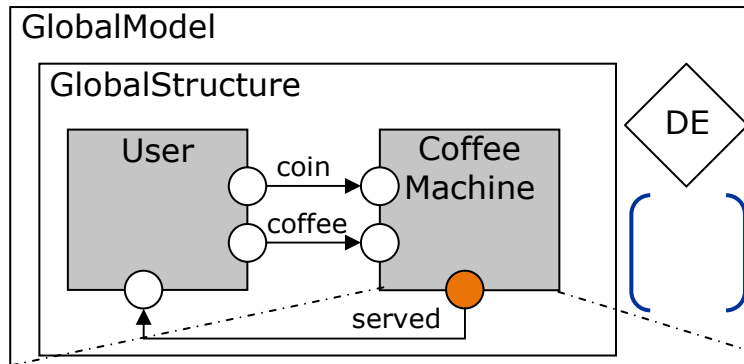
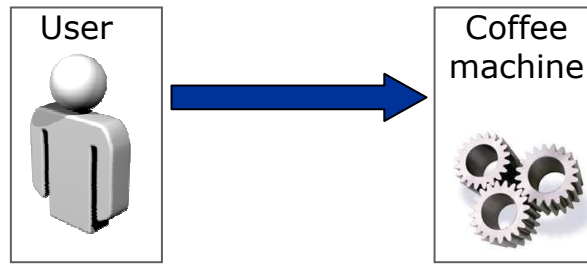
▶ Constraint on the user

■ Second snapshot

▶ $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



CoffeeMachine (InterfaceBlock)

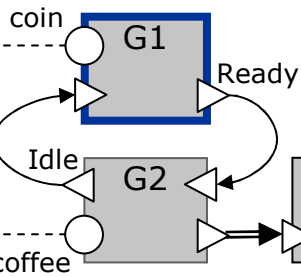
ServingDelay : ΔT

CoffMachModel

CoffMachStructure

init=G1
curr=G1

FSM



■ **Constraint** on the user

■ **First snapshot**

▶ $t_{DE} = 0$

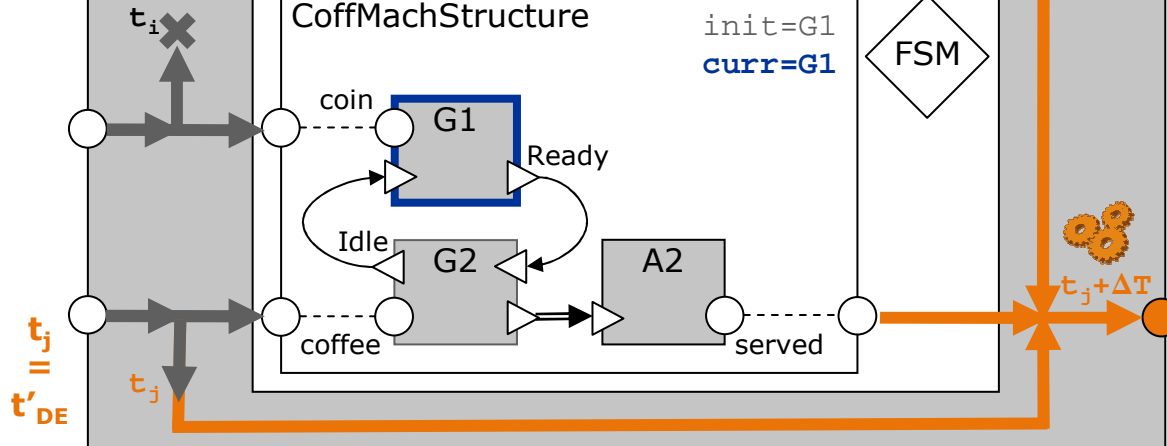
“the user inserts the coin”

▶ **Constraint** on the user

■ **Second snapshot**

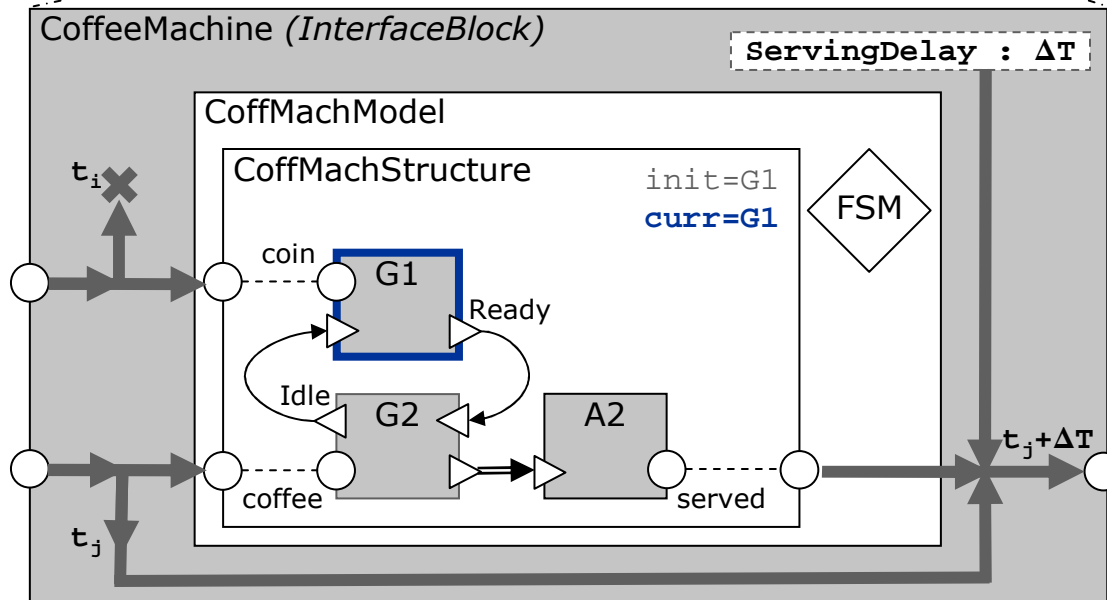
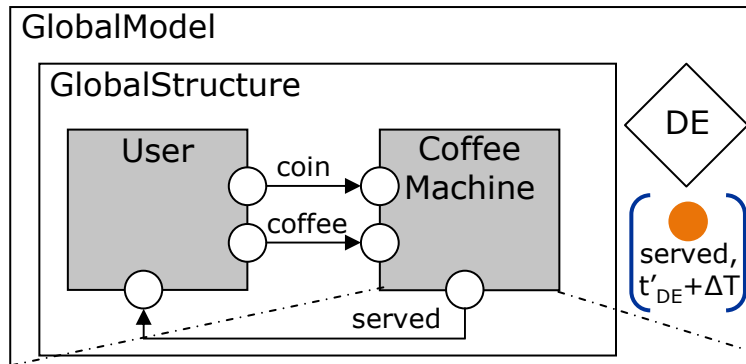
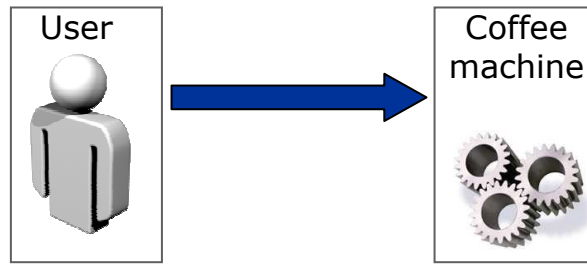
▶ $t'_{DE} = T_{user}$

“the user pushes the button”



$$t_j + \Delta T = t'_{DE} + \Delta T$$

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

“the user inserts the coin”

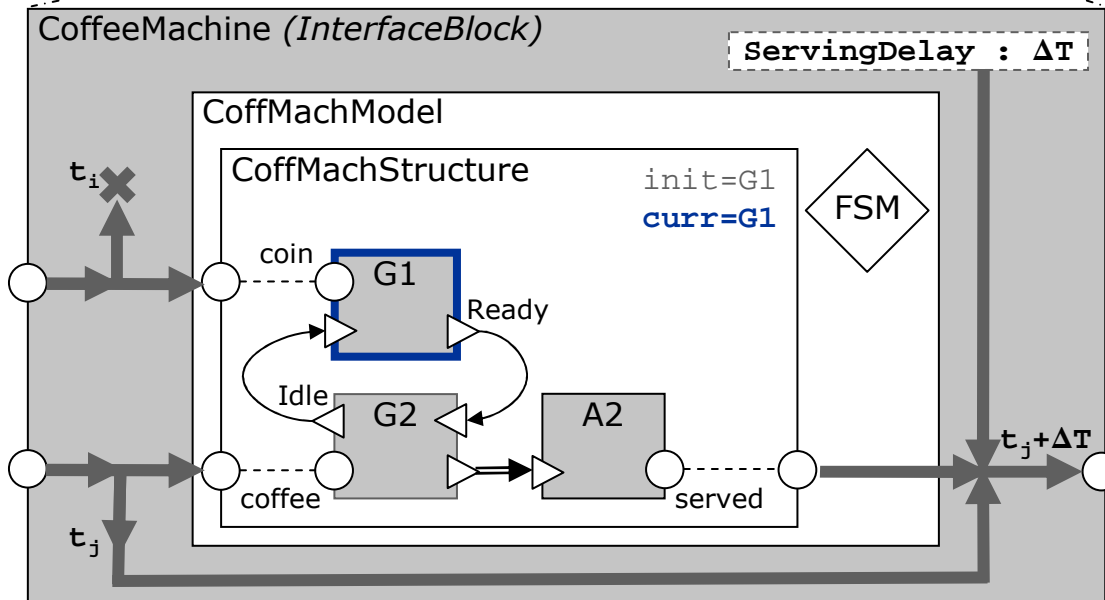
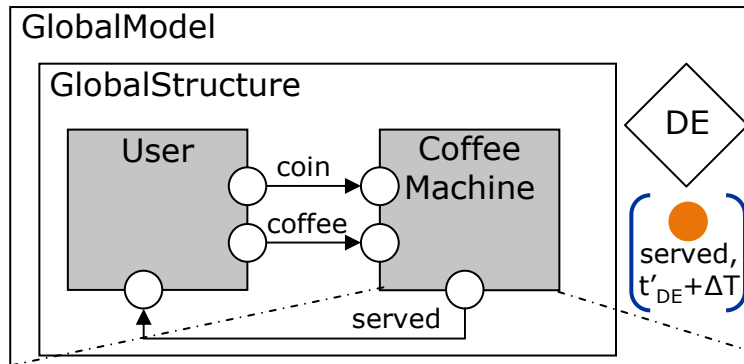
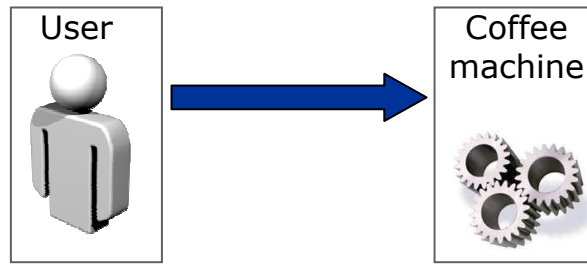
▶ Constraint on the user

■ Second snapshot

▶ $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

► $t_{DE} = 0$

“the user inserts the coin”

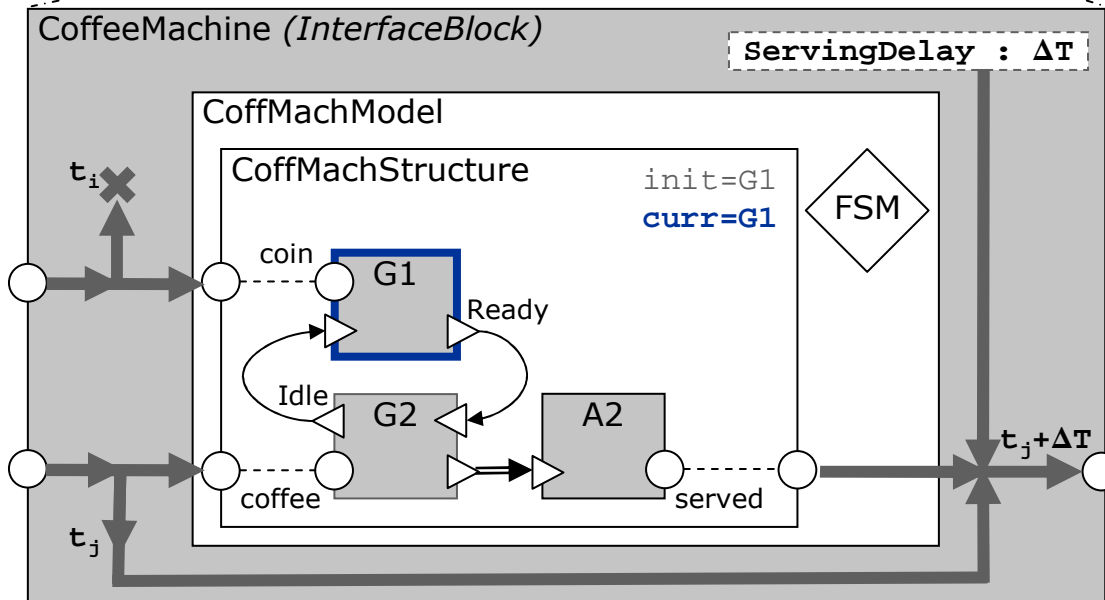
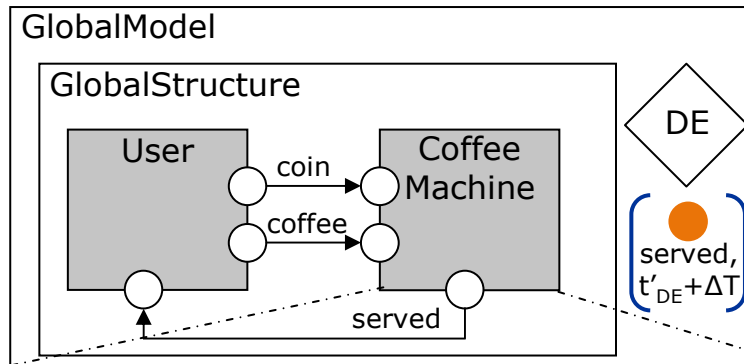
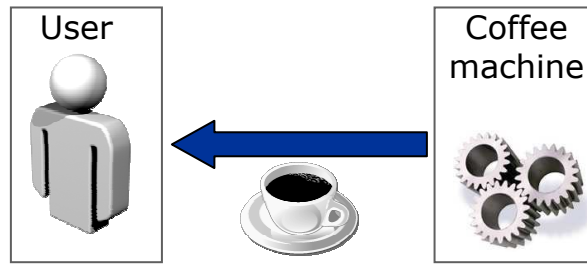
► Constraint on the user

■ Second snapshot

► $t'_{DE} = T_{user}$

“the user pushes the button”

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

“the user inserts the coin”

▶ Constraint on the user

■ Second snapshot

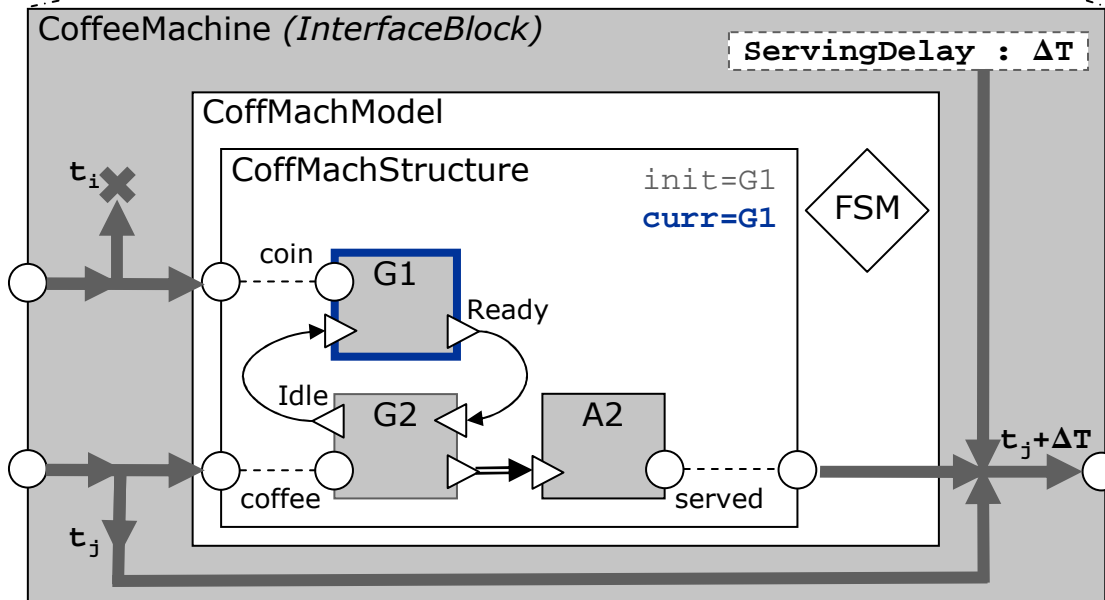
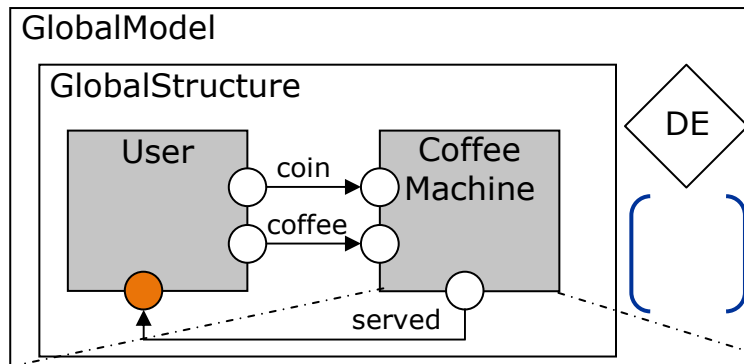
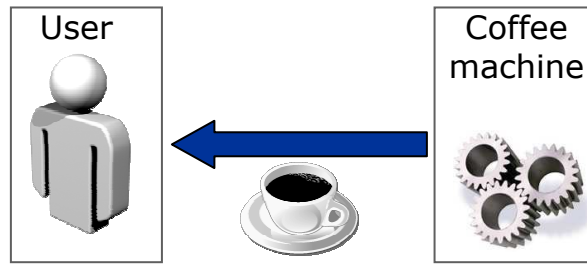
▶ $t'_{DE} = T_{user}$

“the user pushes the button”

■ Third snapshot

▶ $t''_{DE} = t'_{DE} + \Delta T$

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

“the user inserts the coin”

▶ Constraint on the user

■ Second snapshot

▶ $t'_{DE} = T_{user}$

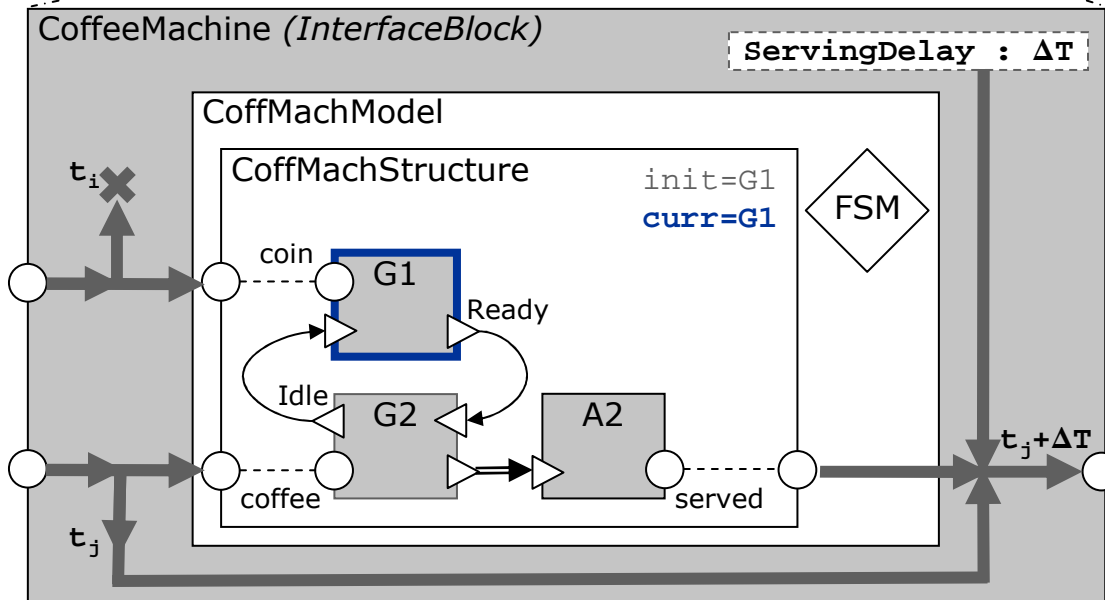
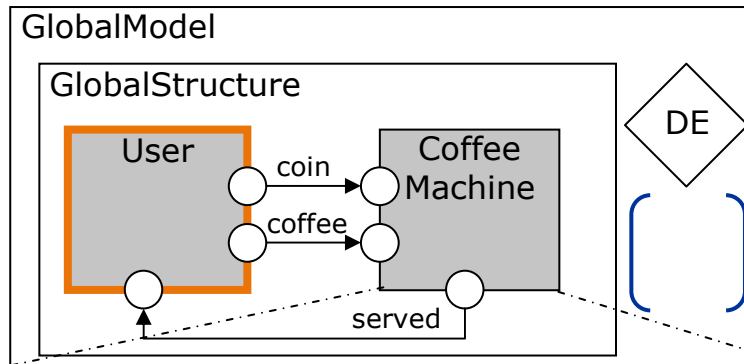
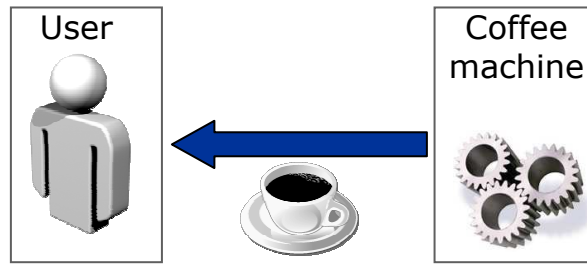
“the user pushes the button”

■ Third snapshot

▶ $t''_{DE} = t'_{DE} + \Delta T$

“the machine delivers the coffee”

Running the model



■ Constraint on the user

■ First snapshot

▶ $t_{DE} = 0$

“the user inserts the coin”

▶ Constraint on the user

■ Second snapshot

▶ $t'_{DE} = T_{user}$

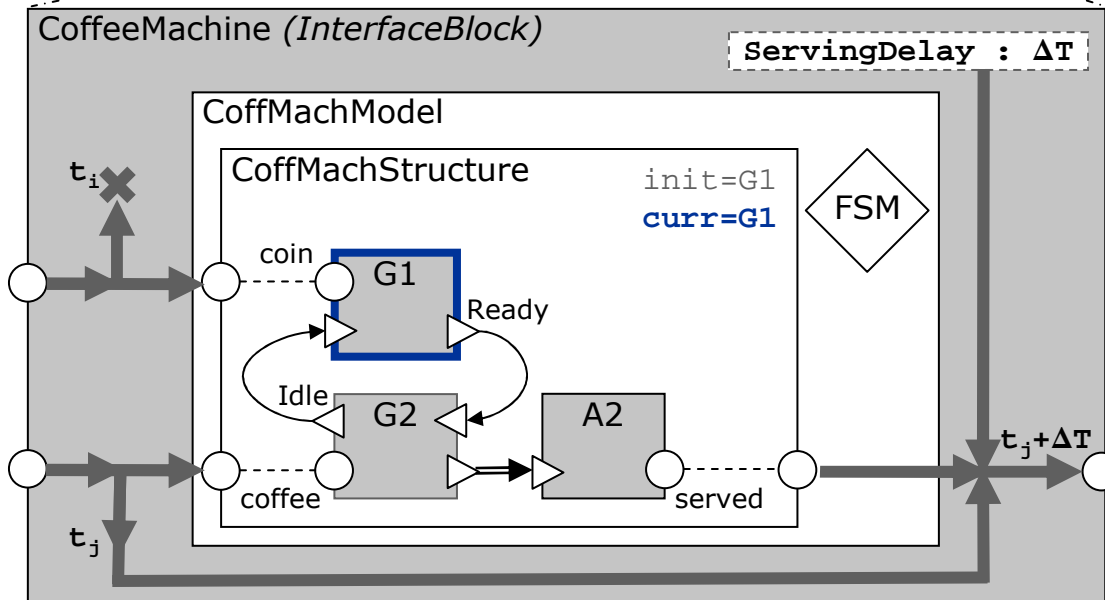
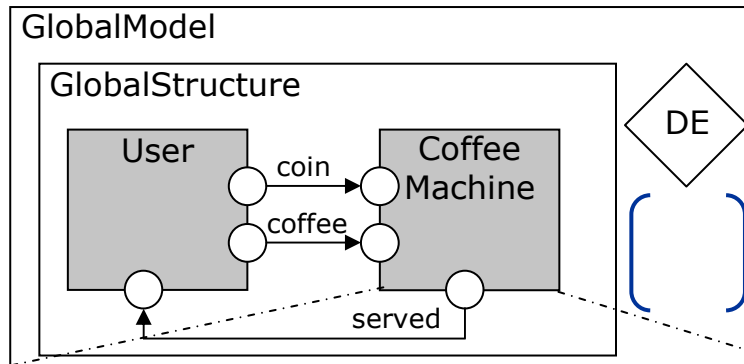
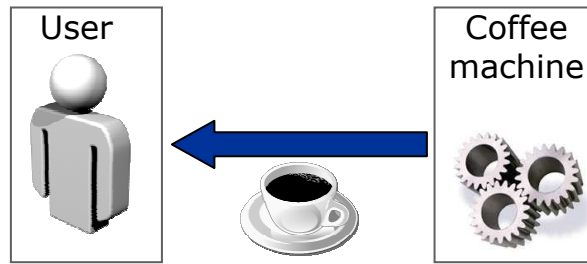
“the user pushes the button”

■ Third snapshot

▶ $t''_{DE} = t'_{DE} + \Delta T$

“the machine delivers the coffee”

Running the model



■ Constraint on the user

■ First snapshot

► $t_{DE} = 0$

“the user inserts the coin”

► Constraint on the user

■ Second snapshot

► $t'_{DE} = T_{user}$

“the user pushes the button”

■ Third snapshot

► $t''_{DE} = t'_{DE} + \Delta T$

“the machine delivers the coffee”

